

Modelling and Experimenting with ITER: the MHD Challenge

by
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with

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Contents

- Introduction to DIII-D development of **ITER and FNSF scenarios**
- Making progress by **integrating experiments and modelling**
 - Understanding and projecting MHD stability limits
 - MHD spectroscopy to measure the approach to a limit
- The **ITER Baseline Scenario**: moderate β_N , zero torque
- The **path to high β_N and steady-state conditions**
 - Modeling the approach to the no-wall limit with non-ideal effects (MARS-K)
- The **steady-state hybrid scenario: high β_N , high torque**
 - Enhance the ideal and resistive limits with profiles and shape changes
- **Low torque at high β_N**
 - Validation of MARS-K description of the rotation effects
- **Discussion**

Goals and Needs of a Fusion Reactor

Large $nT\tau_E$	Need high T_e, T_i
Good confinement (τ_E)	To have high fusion gain $Q = P_{fus}/(P_{input}-P_\alpha)$
Fully non-inductive conditions	For continuous operation (no transient J_{ohm})
High pressure (β_N)	For large J_{boot} , low P_{input}
Long stable plasmas	Avoid disruptions, loss of confinement

How Do We Project Present Experiments to Future Machines?

- Produce demonstrations of relevant conditions in present machines
- Extrapolate to conditions not presently attainable

	PRESENT	FUTURE
EXPERIMENT	<ul style="list-style-type: none">- Plasmas on 1 machine- Multi-machine campaigns	<ul style="list-style-type: none">- Scaling laws
MODELS	<ul style="list-style-type: none">- Benchmark- Validation	<ul style="list-style-type: none">- Predictive capability

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One of the Issues for All the Present Plasmas is Duration at Peak Performance

MHD instabilities cause pressure and rotation collapses, disruptions

- **Ideal kinks, RWMs** → large β_N and rotation collapses, disruptions
- **Tearing (resistive) instabilities** → loss of confinement, disruptions
- **High frequency modes (fishbones, TAEs...)** → loss of confinement, triggering of other modes

Measure the Approach to Instability: MHD Spectroscopy

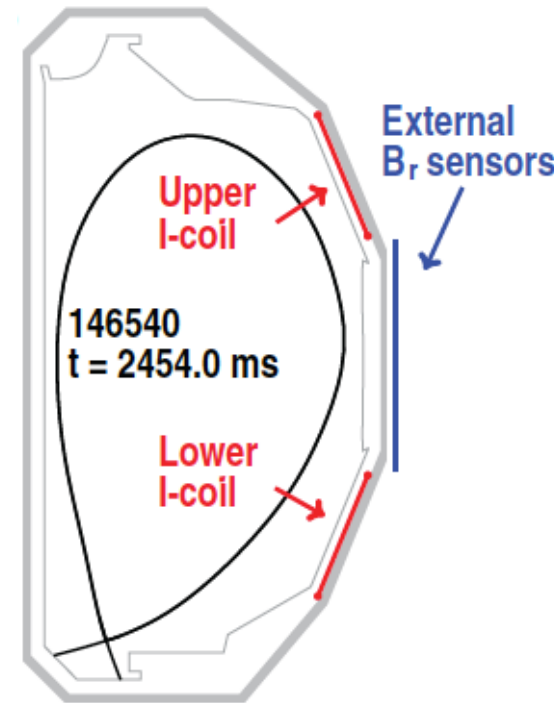
EXP

MHD spectroscopy*: probe the stable side of the RWM

A rotating kink-resonant $n=1$ field is applied with a set of “internal coils” (I-coils), at $f=10$ Hz or $f=20$ Hz \leftarrow rotation frequency of the RWM

- **The plasma response amplitude increases close to a stability boundary**
 - Used to **probe the proximity to an ideal stability limit** (high β_N pressure limit, low q current limit)
 - Resistive stability is strongly correlated to ideal limits* (acquire information on tearing modes)

Expand the analysis and modeling space to the “stable” side of the modes



Rwms as Kink Limit Measured and Modelled With Plasma Response

MOD

- The ideal kink instability, with a realistic (non-ideal) wall model, is described by the RWM branch of the dispersion relation
 - \rightarrow slow growth rate of the order of τ_{wall}
- MHD spectroscopy measures the approach to this stability boundary
- The RWM is influenced by
 - Pressure and current profile gradients (ideal MHD)
 - Resonances between the plasma rotation and the thermal particles drift frequencies
 - Non-resonant contributions from fast-particles (NBI ions in DIII-D)
- In DIII-D, RWMs
 - Cause rotation and β_N collapses in the high- q_{min} , high- β_N SS plasmas
 - Provide the hard disruptive limit in the $q < 2$ scenarios

Drift Kinetic Effects Are Needed to Describe the Experimental Observations

MOD

- RWMs do not usually appear in fast-rotating, low q_{\min} plasmas \rightarrow kinetic damping of the RWM [Hu et al, PRL2004]

$$\gamma\tau_W = -\frac{\partial W_{no-wall}}{\partial W_{ideal-wall}}$$

Ideal MHD RWM dispersion relation

$$\gamma\tau_W = -\frac{\partial W_{no-wall} + \partial W_{kinetic}}{\partial W_{ideal-wall} + \partial W_{kinetic}}$$

Kinetic damping physics

- The rotation, the thermal and fast-ion dependences may extrapolate unfavourably to machines with **low external torque and lower fraction of fast beam-generated ions**, such as ITER

MARS-K Model is Being Validated to Predict the Stability in Unexplored Regimes

MOD

Eigenvalue code, modified to solve for the response to an inhomogeneous forcing function \leftarrow External field from the I-coils

$$\xi(\gamma + i\Omega) = v + (\xi \cdot \nabla \Omega) R$$

Plasma displacement

$$\rho(\gamma + i\Omega)v = -\nabla \cdot p + j \times B + J \times \tilde{B} - \rho(\Omega \times v + v \cdot \nabla \Omega)$$

Momentum (with rotation)

$$(\gamma + i\Omega)\tilde{B} = \nabla \times (v \times B) + (\tilde{B} \cdot \nabla \Omega) R$$

Faraday's law

$$j = \nabla \times \tilde{B}$$

Ampère's

$$(\gamma + i\Omega)p = -v \cdot \nabla P$$

Perturbed pressure

$$p = pI + p_{||} + p_{\perp} \quad \leftarrow \int Mv^2 f d\Gamma$$

Drift kinetic pressure tensors

The model includes

- resistive DIII-D wall geometry
- fast-NBI ions with a Maxwellian slowing down distribution function in y



*Y. Liu et al, Phys. Plasmas 15, 112503 (2008)

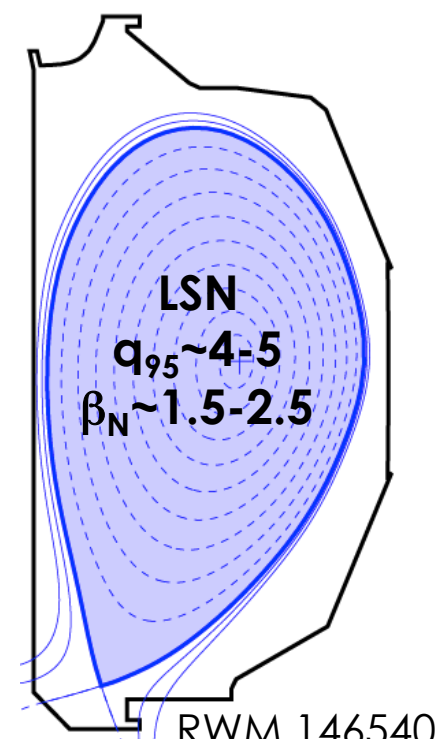
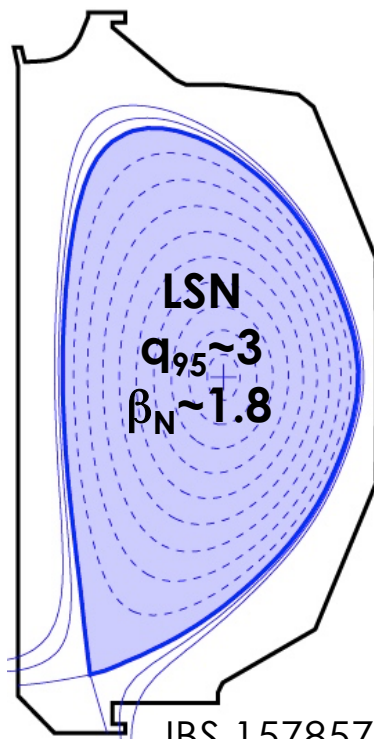
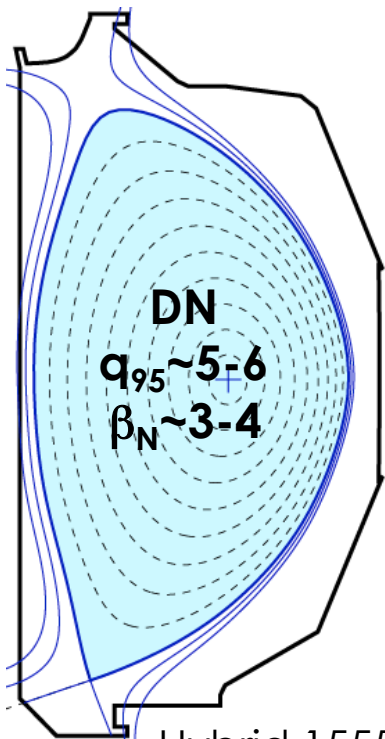
DIII-D is Tasked to Provide Demonstration Plasmas for ITER and FNSF

EXP

Experiments → platform to study the phenomena that the **models** describe

SCENARIO: a type of plasma, and plasma evolution, that has specific requirements for

- plasma shape, q_{95} , Q , torque, collisionality, T_e/T_i , etc



I Am Going to Discuss the Work Towards These Scenarios:

ITER	ITER Baseline Scenario (IBS) $Q=10$, 15 MA ($q_{95} \sim 3$), $q_0 < 1$, $P_{fus} = 500$ MW, LSN shape
	Steady-State $Q=5$, 9 MA ($q_{95} \sim 5$), LSN shape, $f_{NI} = 1$
FNSF*	Steady-state $Q < 5$, 6.7 MA, $q_{min} > 1$, DN, high neutron fluence

***Fusion Nuclear Science Facility** for FDF (future US machine) → the mission is to develop fusion blankets and test materials

IBS: MHD Stability Below The No-wall Limit, At Zero Torque

ITER	ITER Baseline Scenario (IBS) Q=10, 15 MA ($q_{95} \sim 3$), $q_0 < 1$, $P_{fus} = 500$ MW, LSN shape
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← $\beta_N \sim 1.8-2.2$

[IBS] Stable Solution Found At Moderate to High Torque

EXP

- **DIII-D IBS demonstration discharges match**

- plasma shape (LSN)

- $q_{95} = 3.1$

(ITER $I_p = 15$ MA, $B_t = 5.3$ T, $R = 6.2$ m)

- $Q = 10 \leftarrow \beta_N = 1.8, H_{98} = 1$ at $q_{95} = 3$

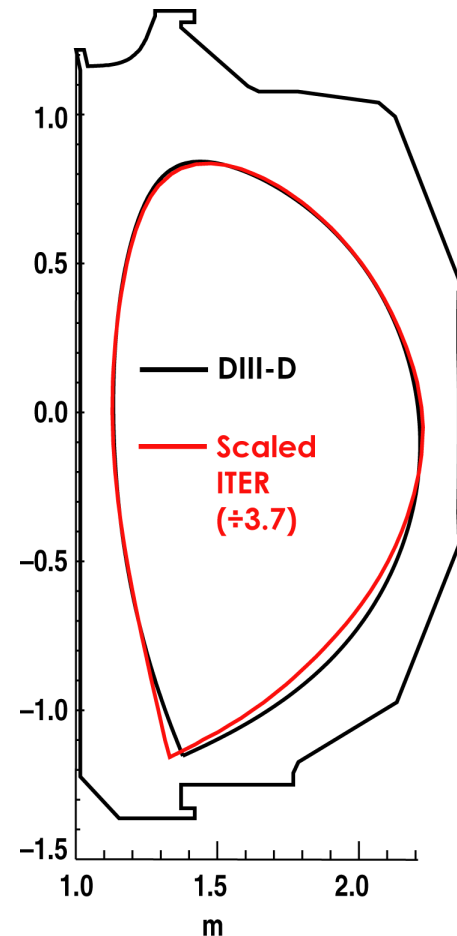
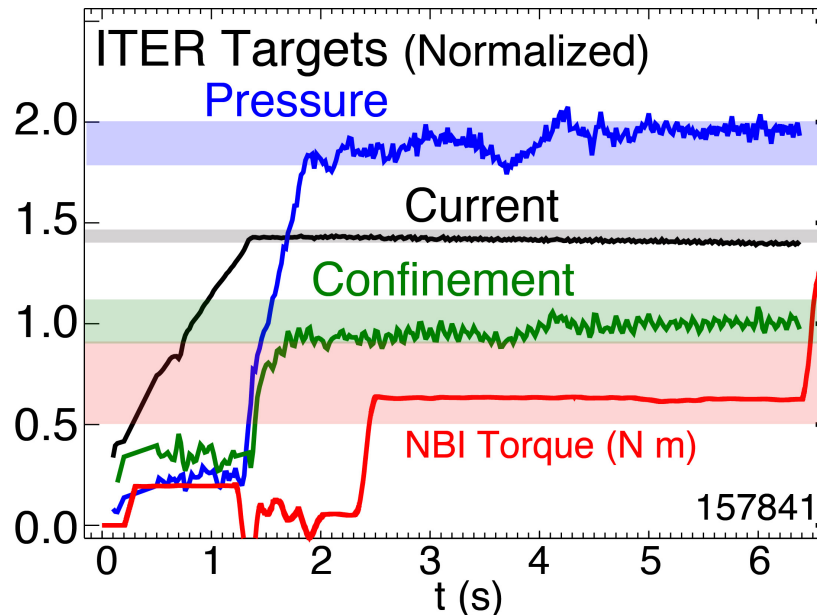
DIII-D can match the predicted torque \rightarrow 0-0.7 Nm

- **Not matching with the present heating systems:**

- $T_e/T_i \sim 0.6-0.9$ at $\rho = 0$

- collisionality

Solution not very reproducible



[IBS] At Low Torque Life is Even Harder

EXP

- Narrow operating point found at ≥ 1 Nm
- Operation at 0 Nm remains elusive
- Modes appear after several τ_E at constant β_N



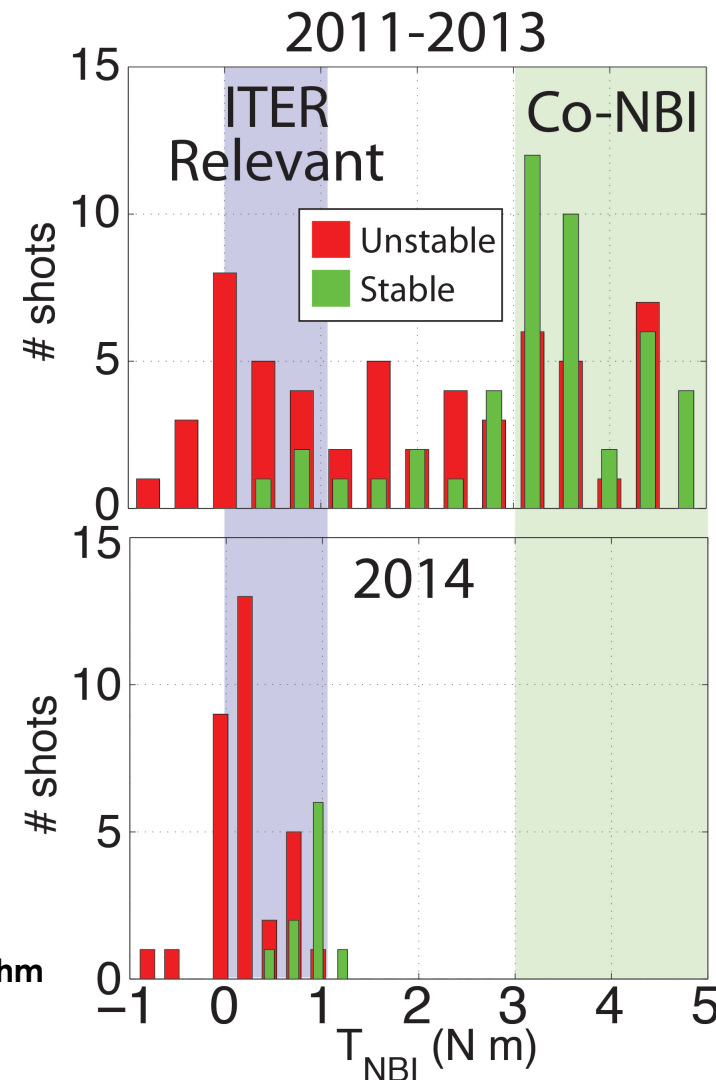
Operating on a marginal point
→ sensitive to small perturbations

Ideal no-wall limit $\beta_{NW} \sim 2.8-3.1$
Ideal with-wall limit $\beta_{WW} \sim 3.2-3.5$
IBS constant $\beta_N \sim 1.8-2.2$

Non-ideal effects → current profile, rotation

Low rotation → more mode coupling, less wall stabilization

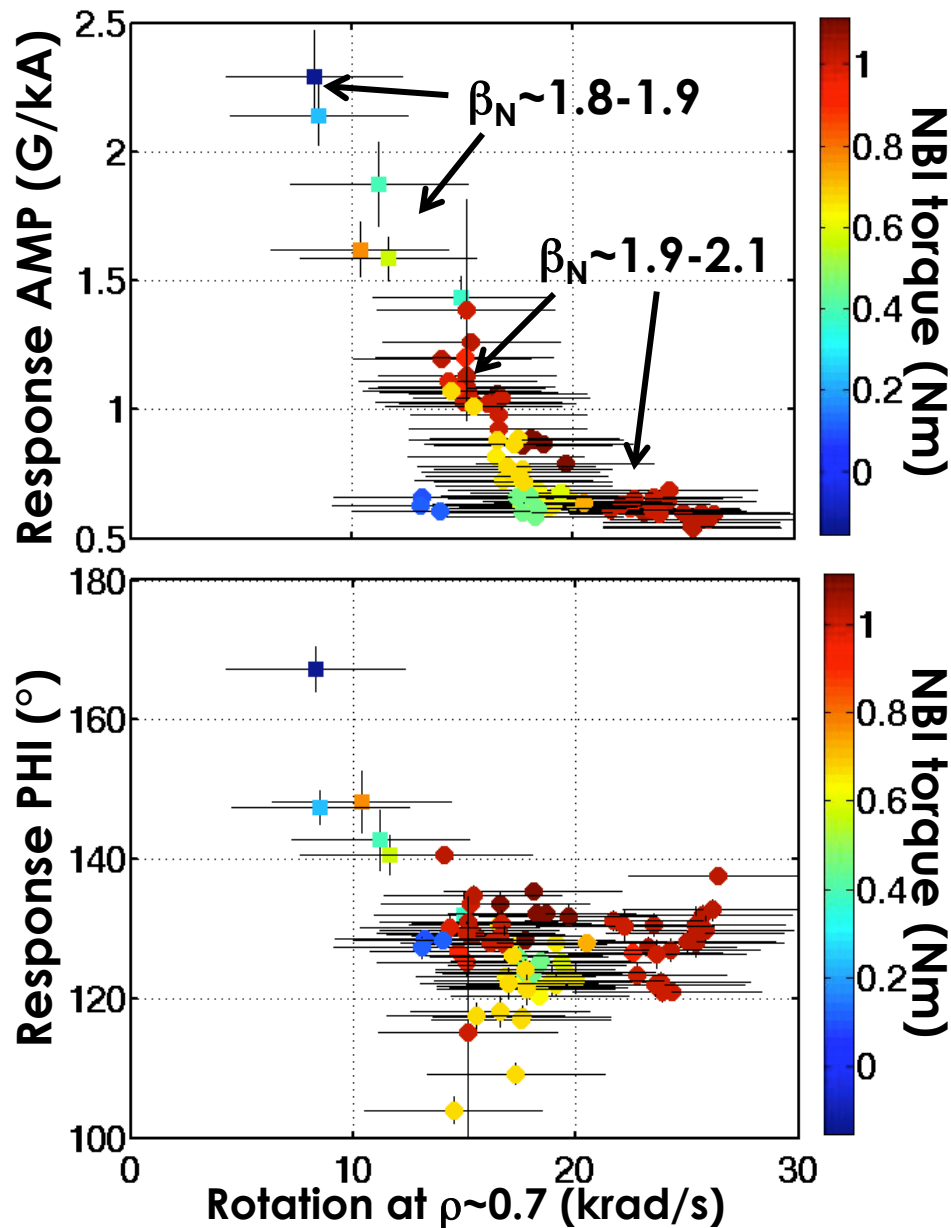
Rotation → transport → T_e → indirectly impacts J_{ohm}
→ current profile more unstable?



MHD Spectroscopy Can Measure the Proximity to A Stability Limit

EXP

Response amplitude increase



MHD Spectroscopy Can Measure the Proximity to A Stability Limit

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Response amplitude increase

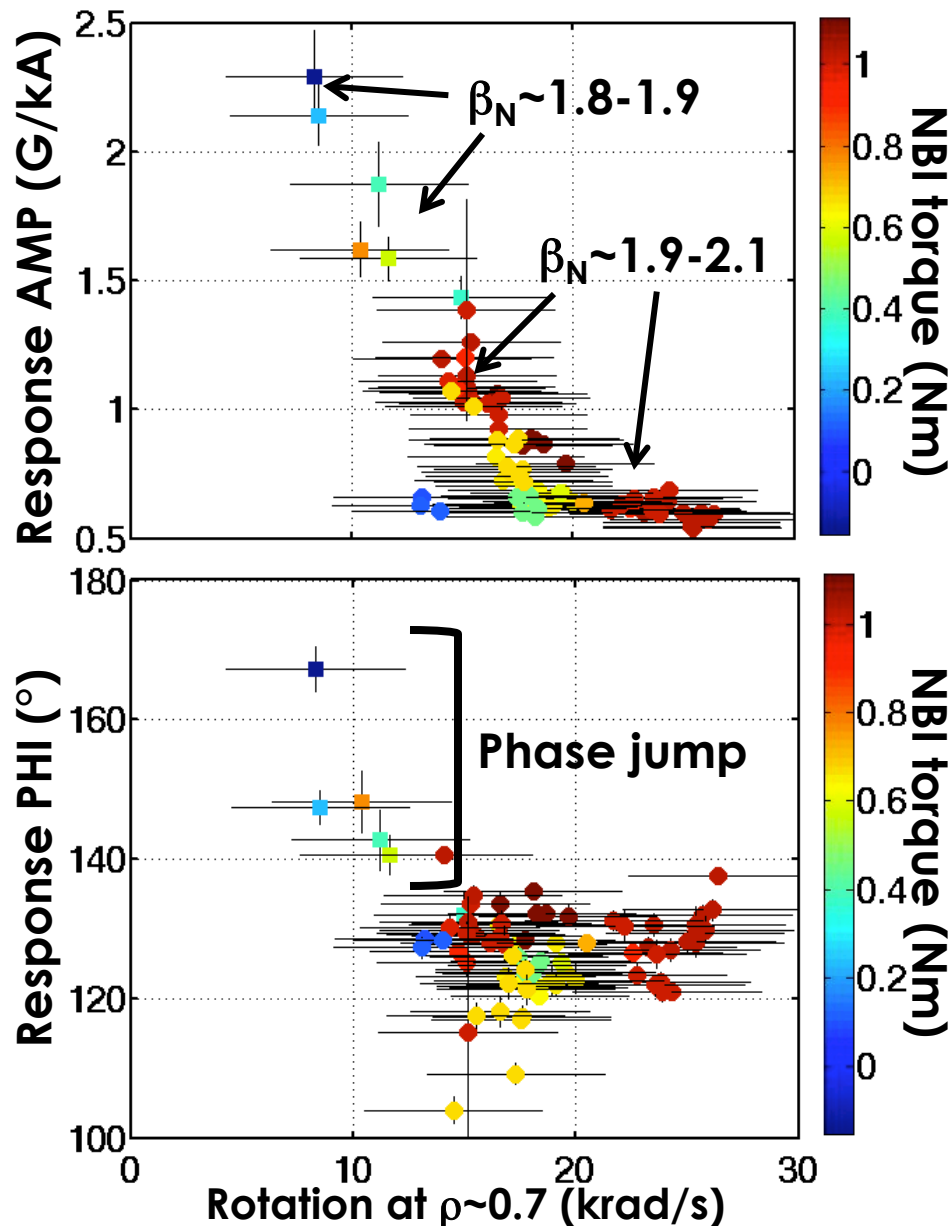


Non-ideal effects \leftrightarrow Lower limits



Phase jump at $\sim 12-15$ krad/s

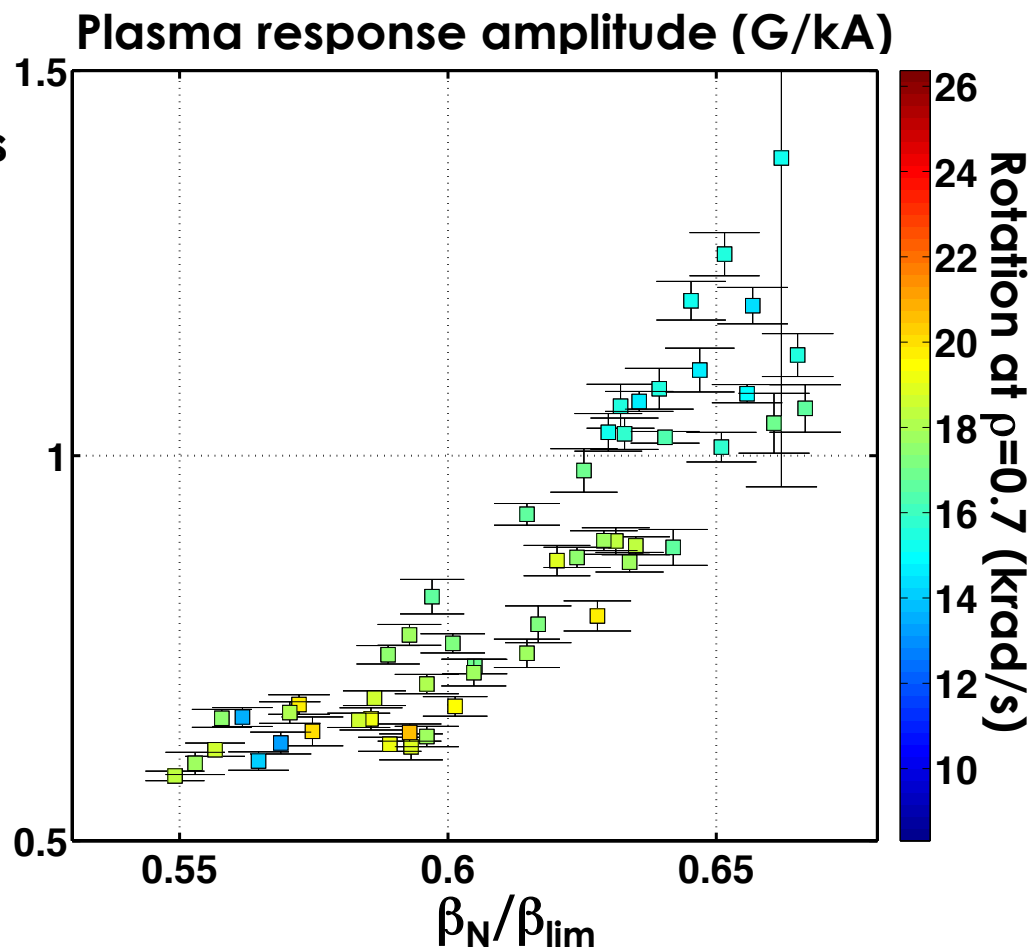
\rightarrow Typical of no-wall limit crossing



MHD Spectroscopy Can Measure the Proximity to A Stability Limit

EXP

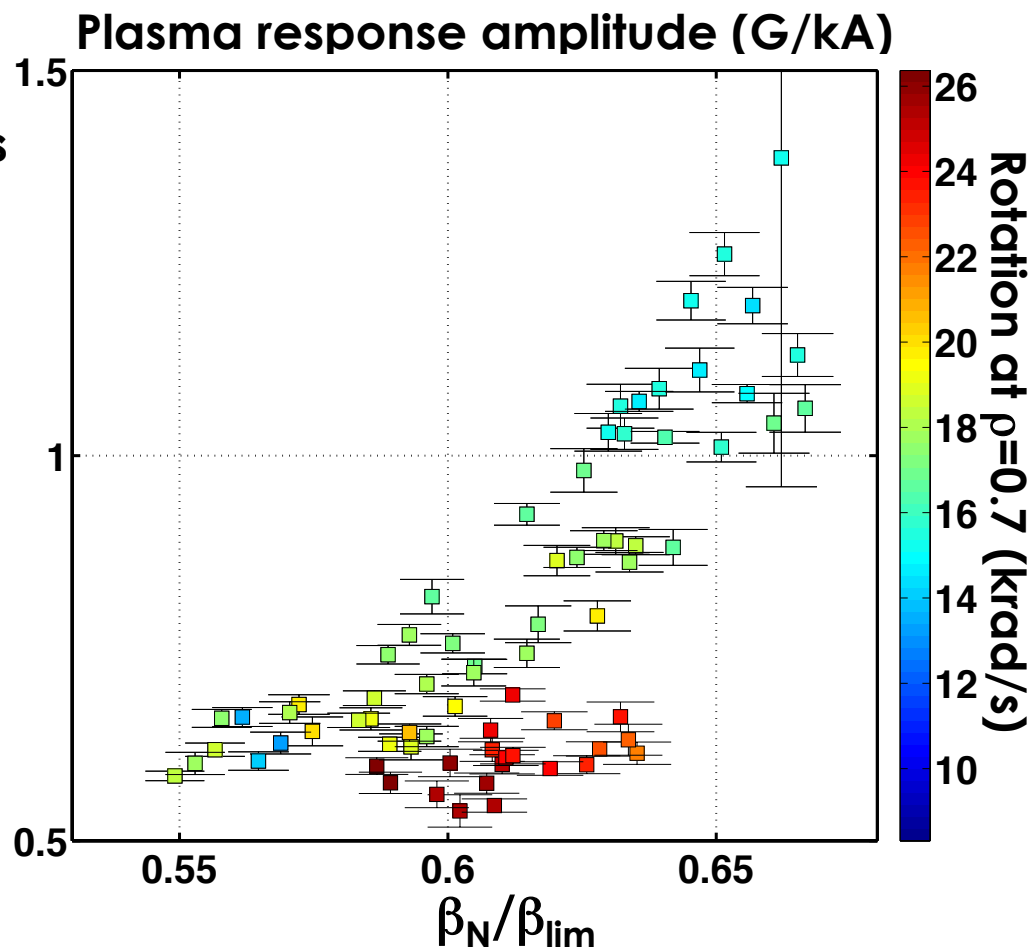
- At “moderate” rotation, the trends are consistent with the ideal model



MHD Spectroscopy Can Measure the Proximity to A Stability Limit

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- At “moderate” rotation, the trends are consistent with the ideal model
- At higher rotation the response is off trend → kinetic damping?



MHD Spectroscopy Can Measure the Proximity to A Stability Limit

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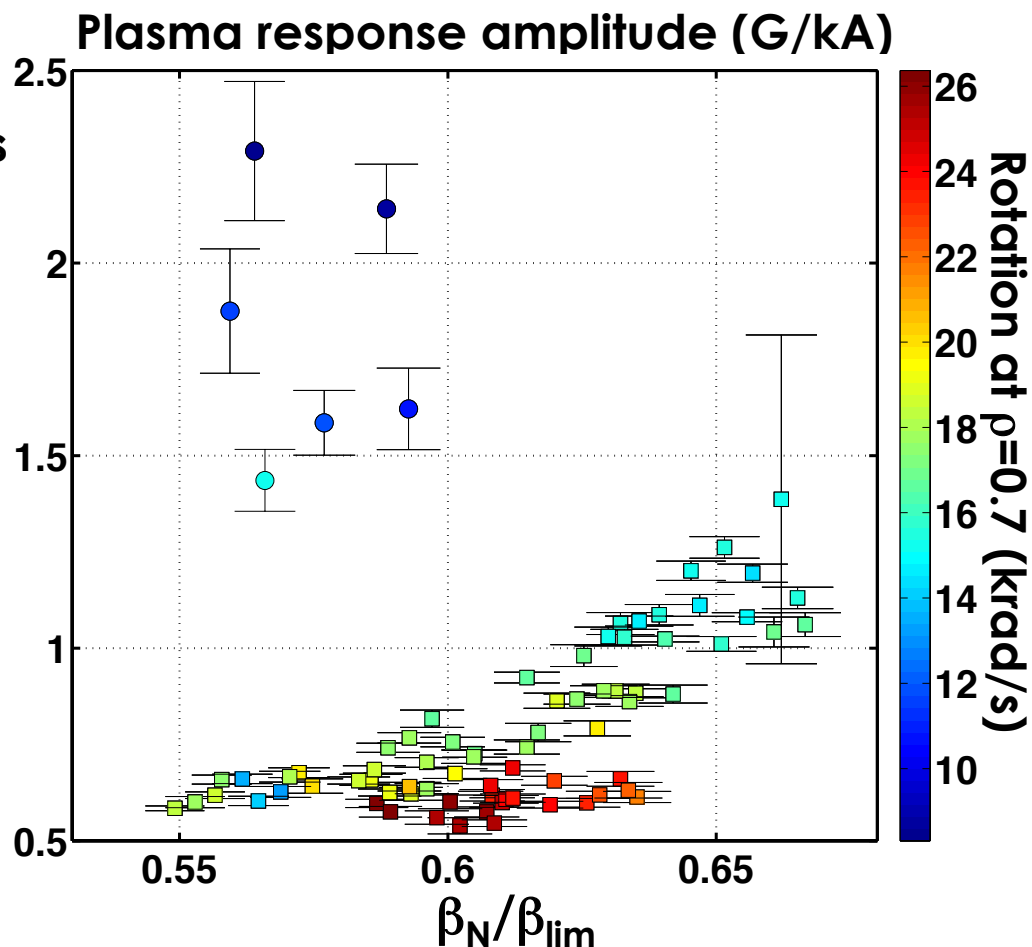
- At “moderate” rotation, the trends are consistent with the ideal model

- At higher rotation the response is off trend → kinetic damping?

- At very low rotation, with ECH, higher response → collisionality effect?



Ideal MHD likely not sufficient to explain the trends



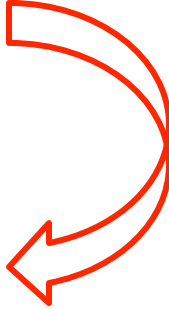
Modeling of rotation and kinetic damping effects



Understand instability at low torque

The Path to High β_N is A Good Platform to Validate Models

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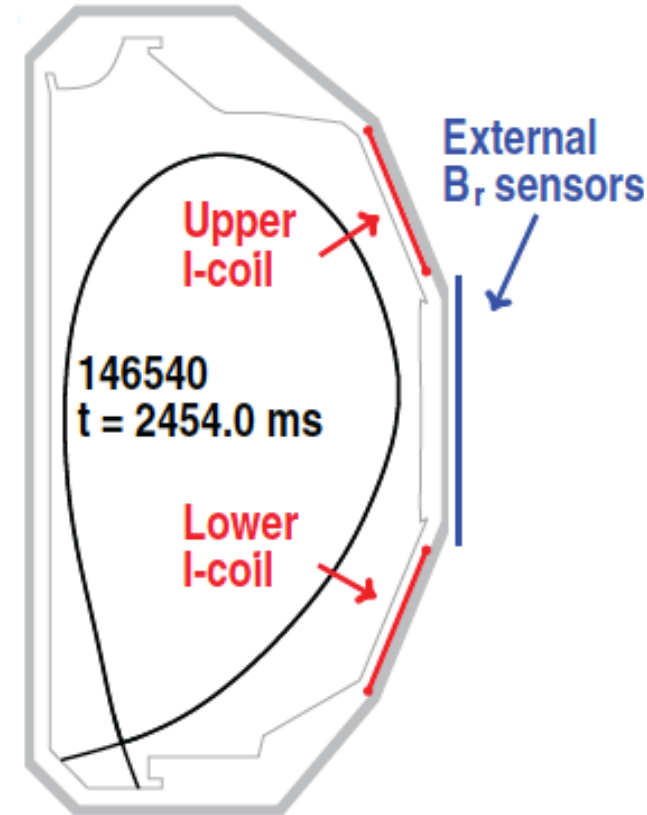
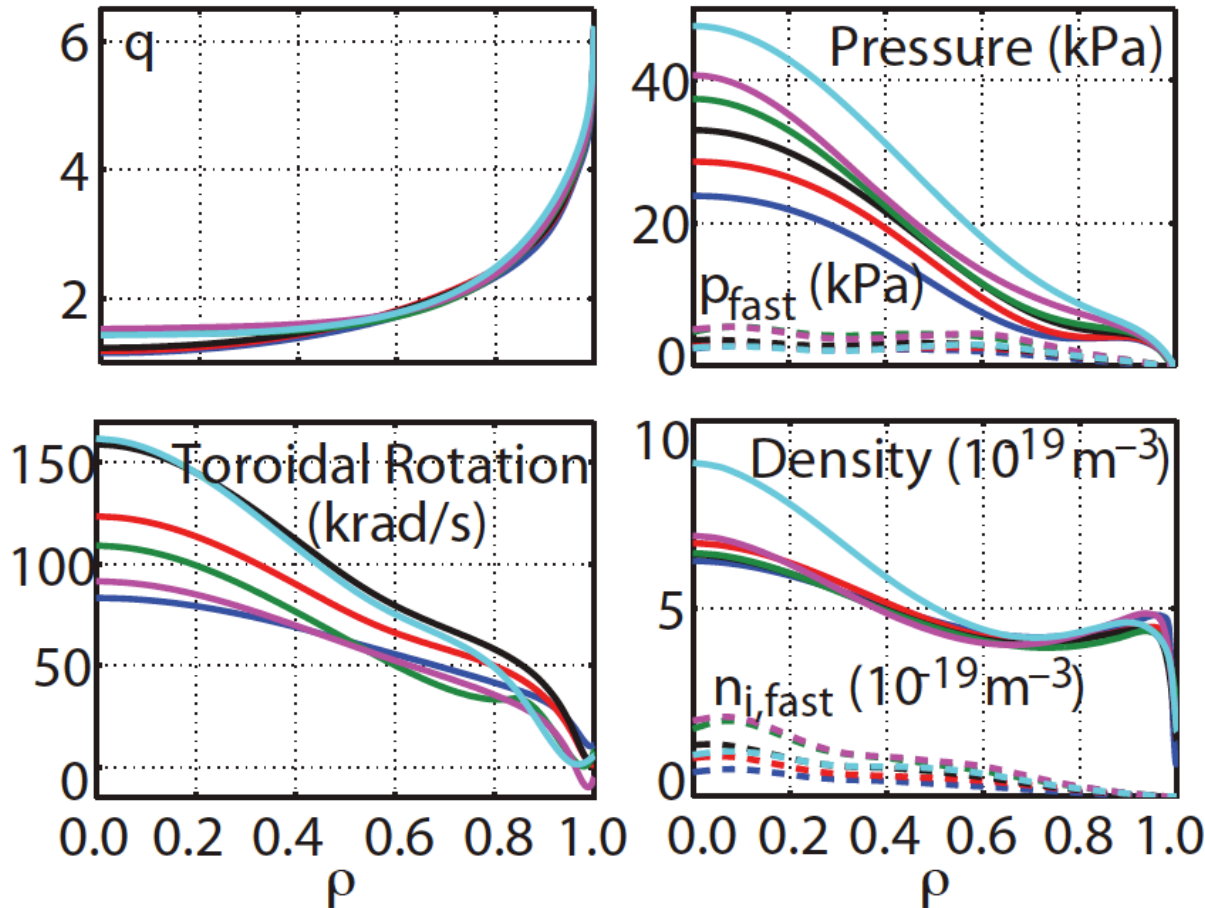


**Higher β_N
Higher q_{95}
RWM plasma**

Experiments: Pressure (β_n) Scan to Cross the No-wall β_n Limit

EXP

Increase the pressure with NBI power \rightarrow Measure the plasma response

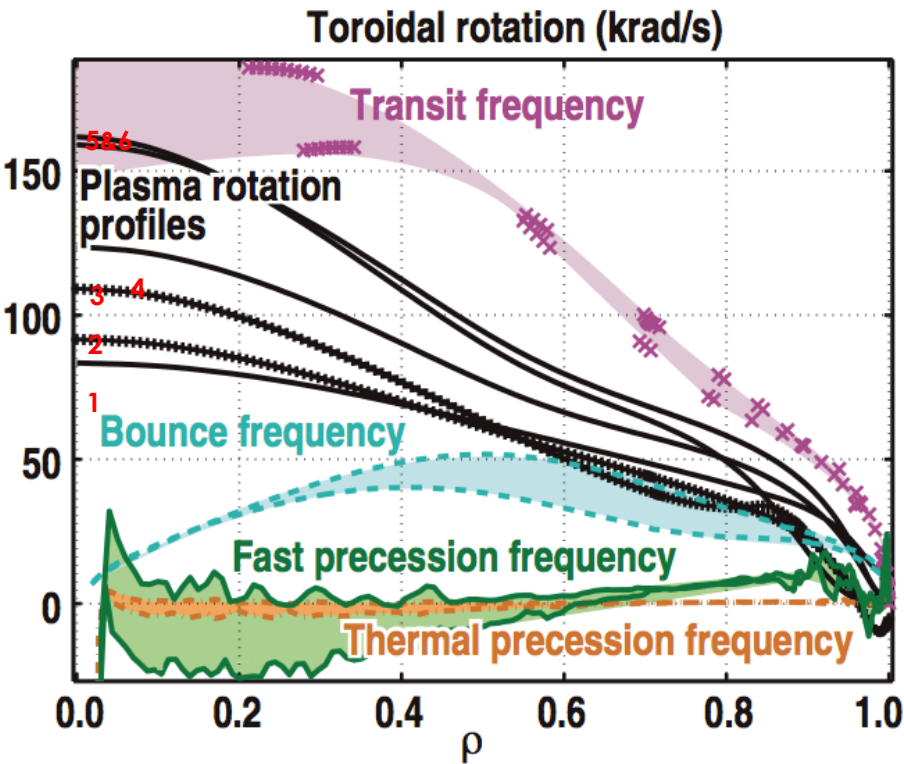


β_n Scan: It's Crucial to Assess the Validity of the Modeling Results

MOD

- Rotation has an impact on the response amplitude
- **The rotation is not constant across the β_N values**

- Some of the variations may be due to the rotation!
- Understand the validity of the results (sensitivity to other variables)



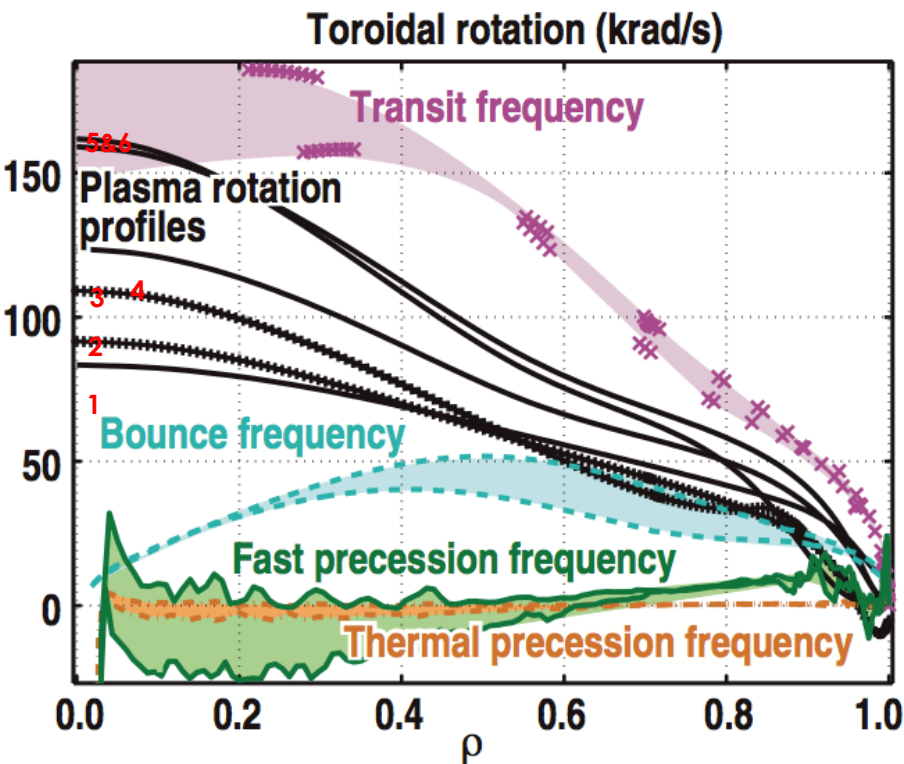
β_n Scan: It's Crucial to Assess the Validity of the Modeling Results

MOD

- Rotation has an impact on the response amplitude
- The rotation is not constant across the β_N values

- Need to isolate the effect of $\beta_N \rightarrow$ keep rotation fixed
- ...for each β_N case:

Sensitivity study:

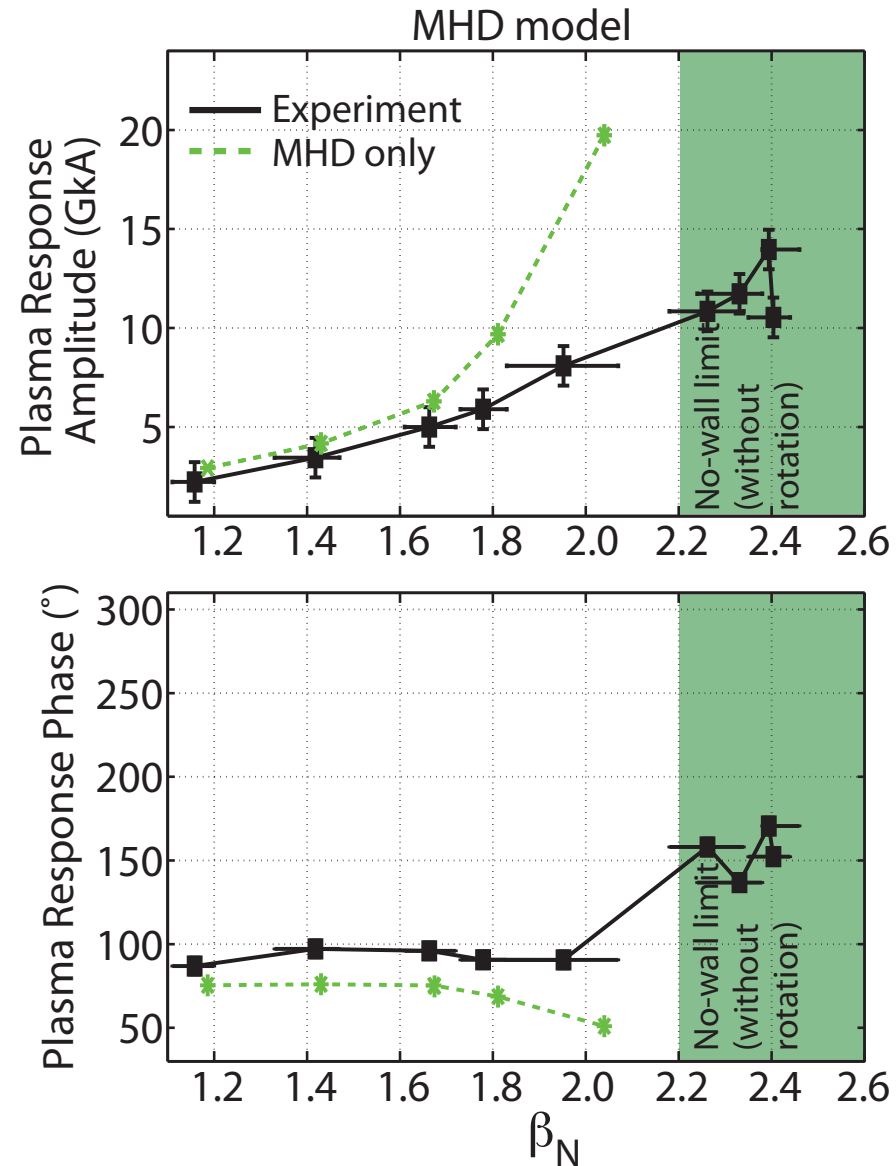


$\Omega \rightarrow$ $\beta_N \downarrow$	1	2	3	4	5	6
1.18	fixed β_N					
1.43						
1.67	fixed Ω					
1.8						
2.05						
2.5						

β_n Scan: MHD-only Model Does Not Reproduce Approach to the No-wall β_n Limit

MOD

- Previous modelling* showed the MHD model without rotation has a pole at the no-wall limit



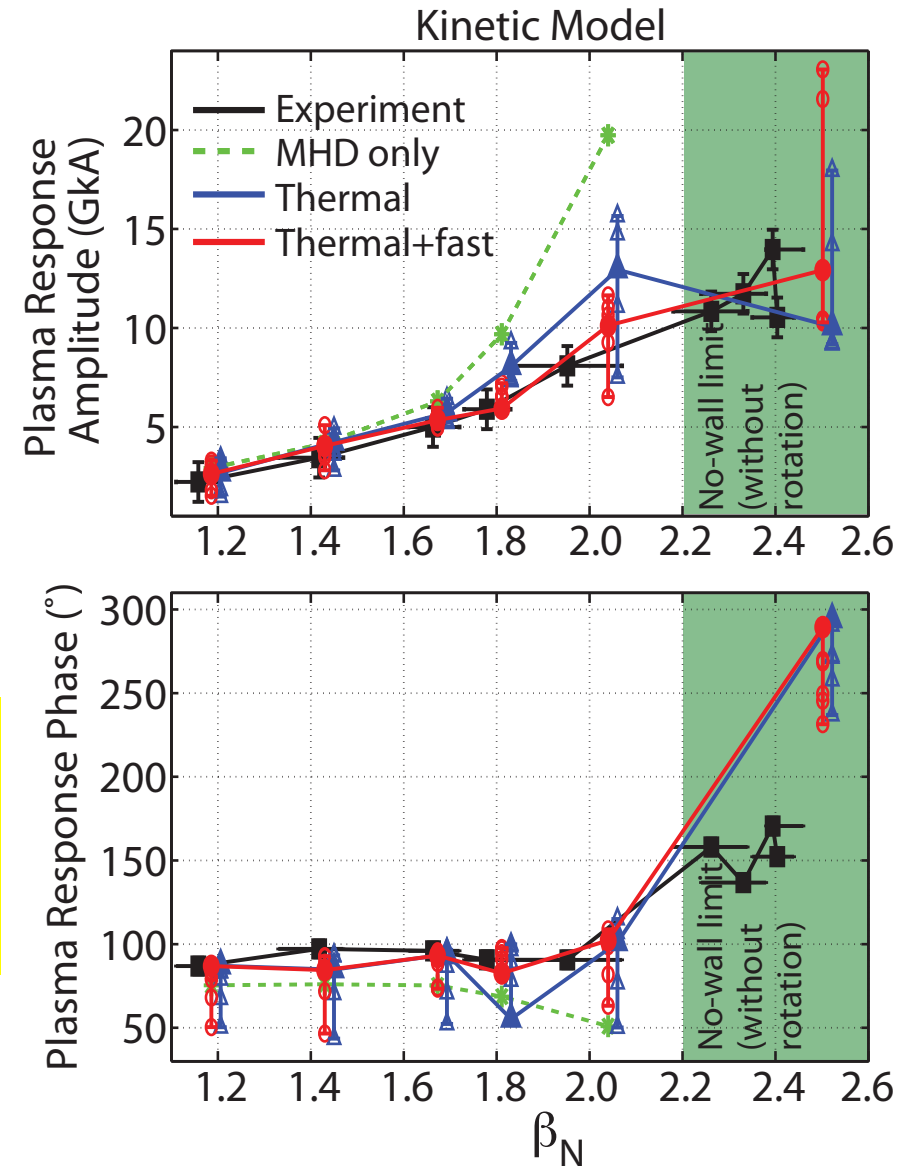
β_n Scan: Drift Kinetic Model Reproduces Approach to the No-wall β_n Limit Correctly

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- Previous modelling* showed the MHD model without rotation has a pole at the no-wall limit
- The pole is eliminated with the full kinetic model (thermal + fast ions)
- Without fast-ion damping the pole reappears \rightarrow 45% higher than expt
- The phase shift is still overestimated above the no-wall limit

The sensitivity study

- Shows how much of the trend is *not* due to the β_N
- Provides confidence in the results



β_n Scan: Drift Kinetic Model Reproduces Approach to the No-wall β_n Limit Correctly

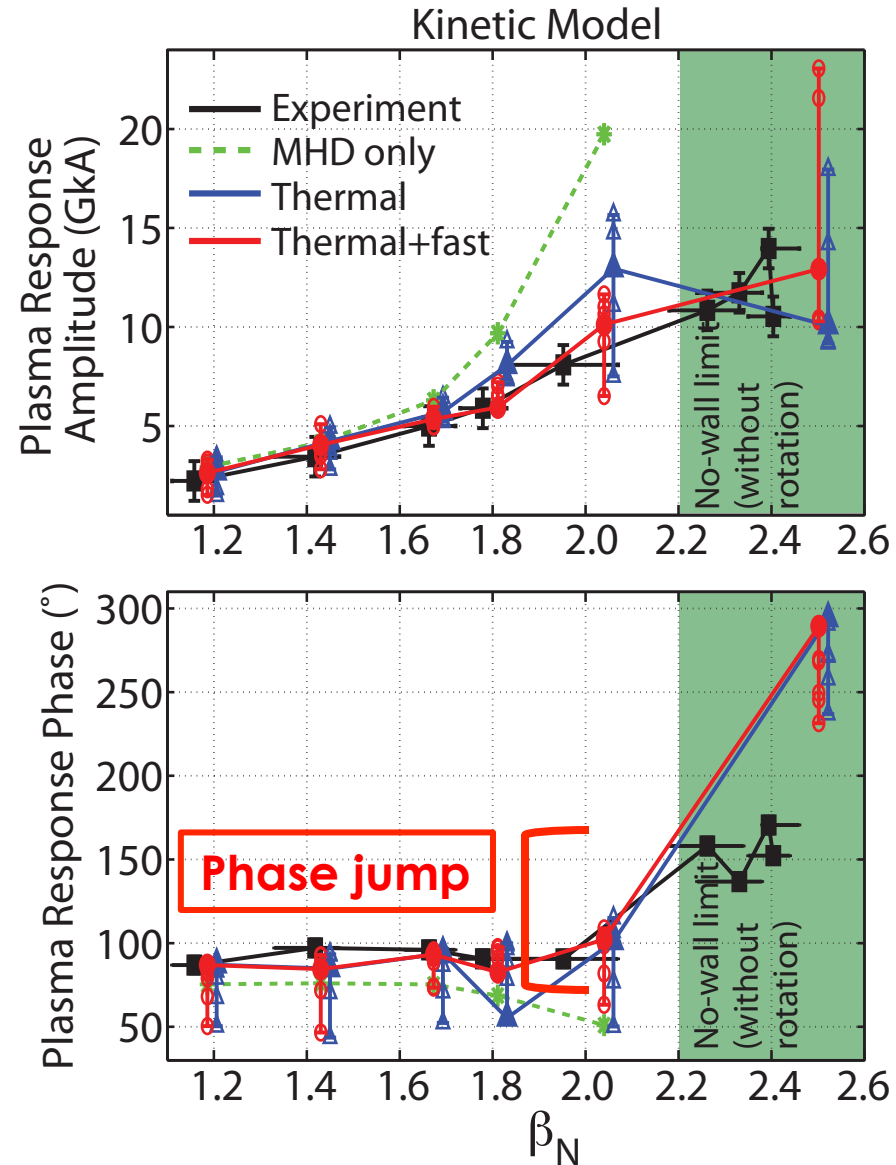
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ITER: very small fast-ion β from NBI

\rightarrow will the plasmas be (45%) more unstable?

\rightarrow Will the fast α -particles be enough to stabilize them?



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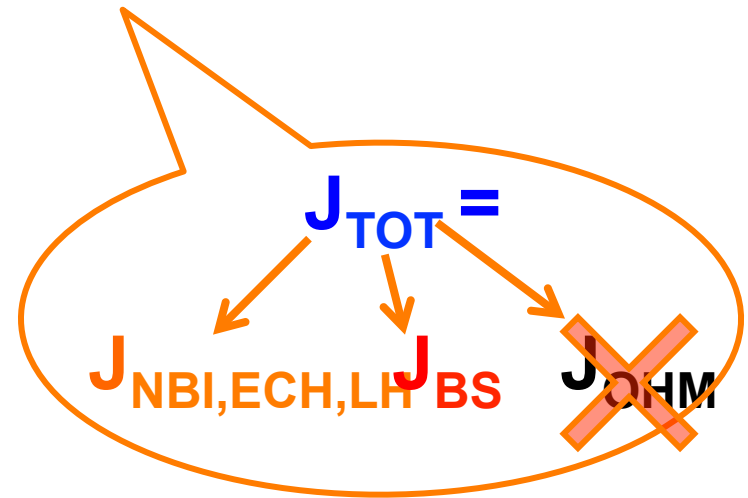
} $\beta_N \sim 3-4$

Steady-state: Fully Non-inductive Current Drive, Where the Plasma Current and Pressure Have Stopped Evolving (Reached A Stable State)

- Current must be composed of bootstrap and externally driven NBI, ECH...
- Large J_{boot} is associated to high β_N



- MHD stability can be an issue even at high torque



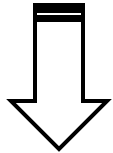
- Standard high- β_N , steady-state scenario \rightarrow high $q_{\text{min}} \sim 1.5-2.5$, zero/reversed shear, broad profiles with off-axis CD

...or not!

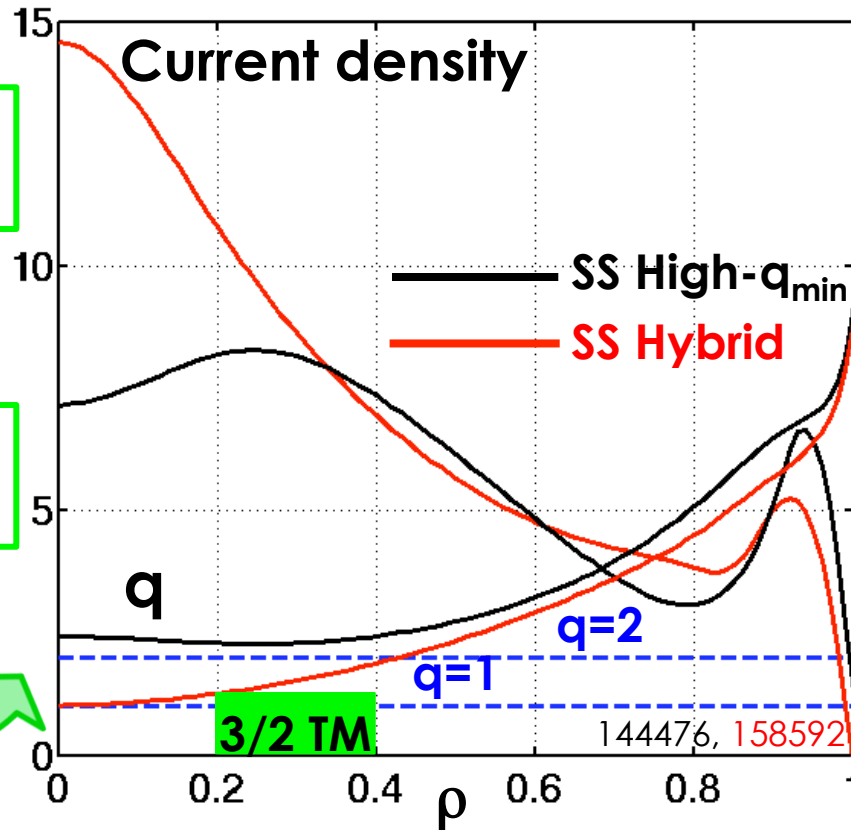
Alternative Approach: the Hybrid Scenario

What is a hybrid? → Long duration, high confinement H-mode
→ More stable to 2/1 tearing modes

Final J independent
from sources



q relaxes to "hybrid"
state - $q_{\min} \geq 1$

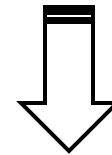


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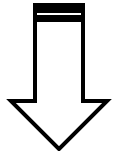
→ More stable to 2/1 tearing modes

All external current driven
in the plasma centre

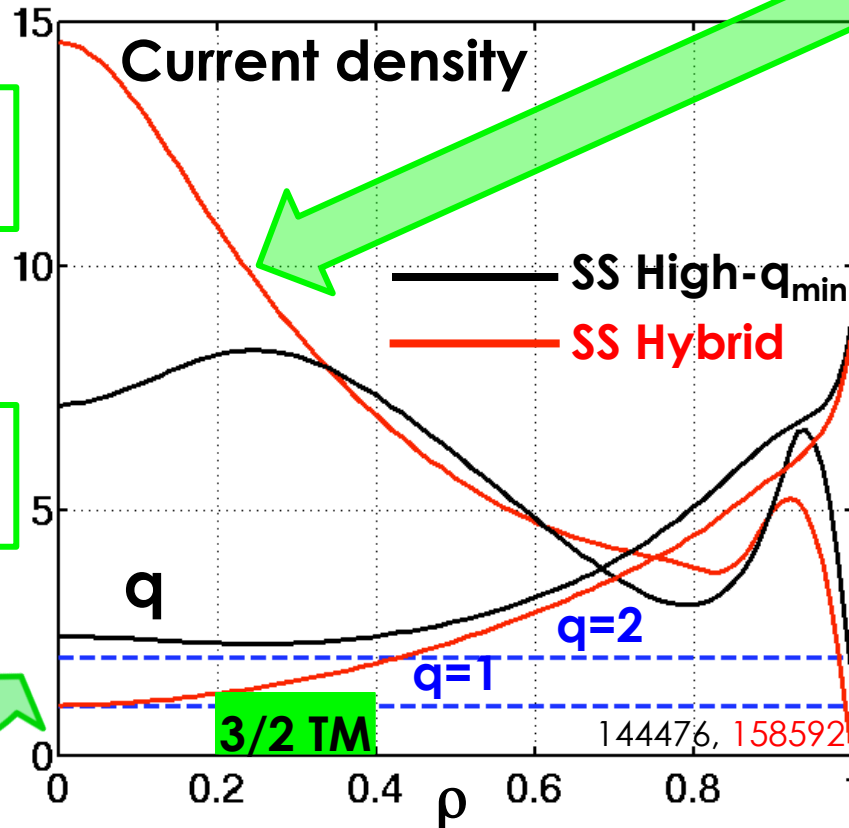


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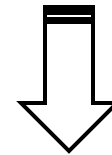
- Benign $m=3/n=2$ or $m=4/n=3$ mode causes "flux pumping" out of $\rho \sim 0.35$
- q naturally stays above 1 → no sawteeth

Alternative Approach: the Hybrid Scenario

What is a hybrid? → Long duration, high confinement H-mode

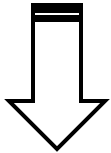
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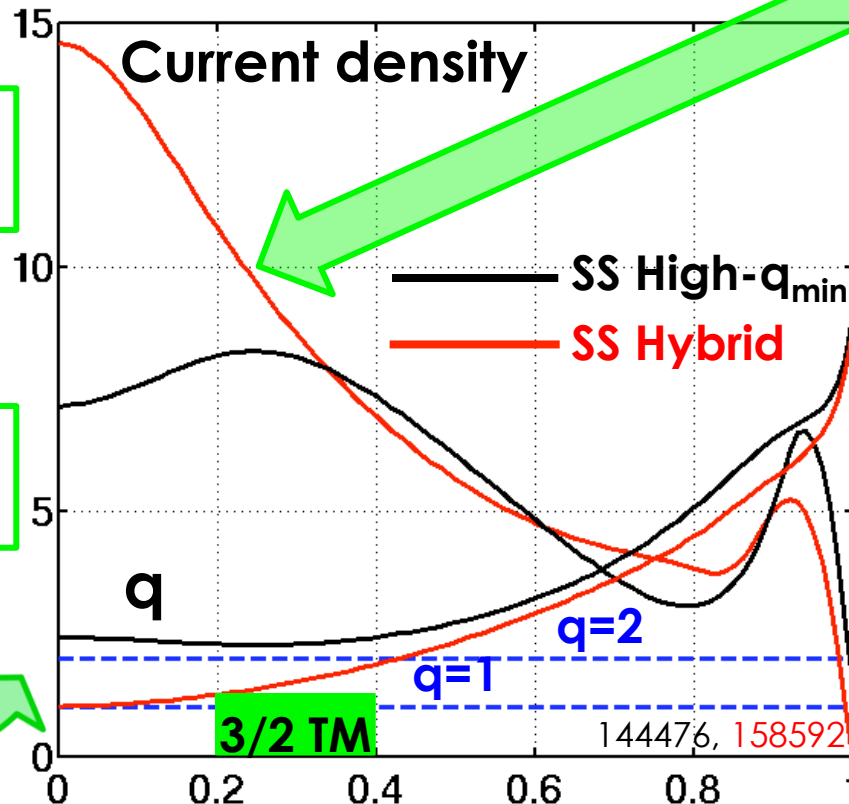


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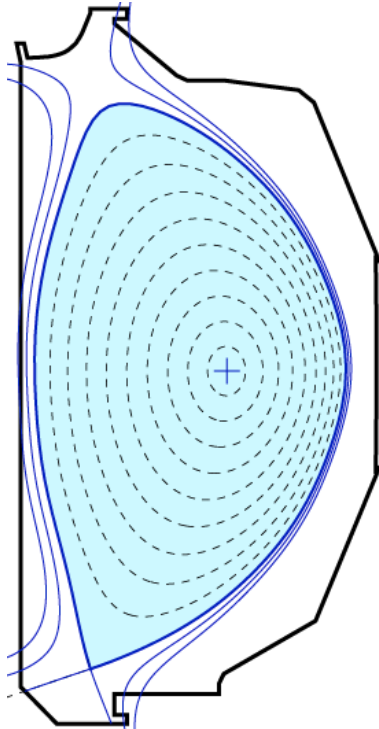


Ideal MHD with-wall limits are $\beta_{\text{limit}} \geq 4.5$

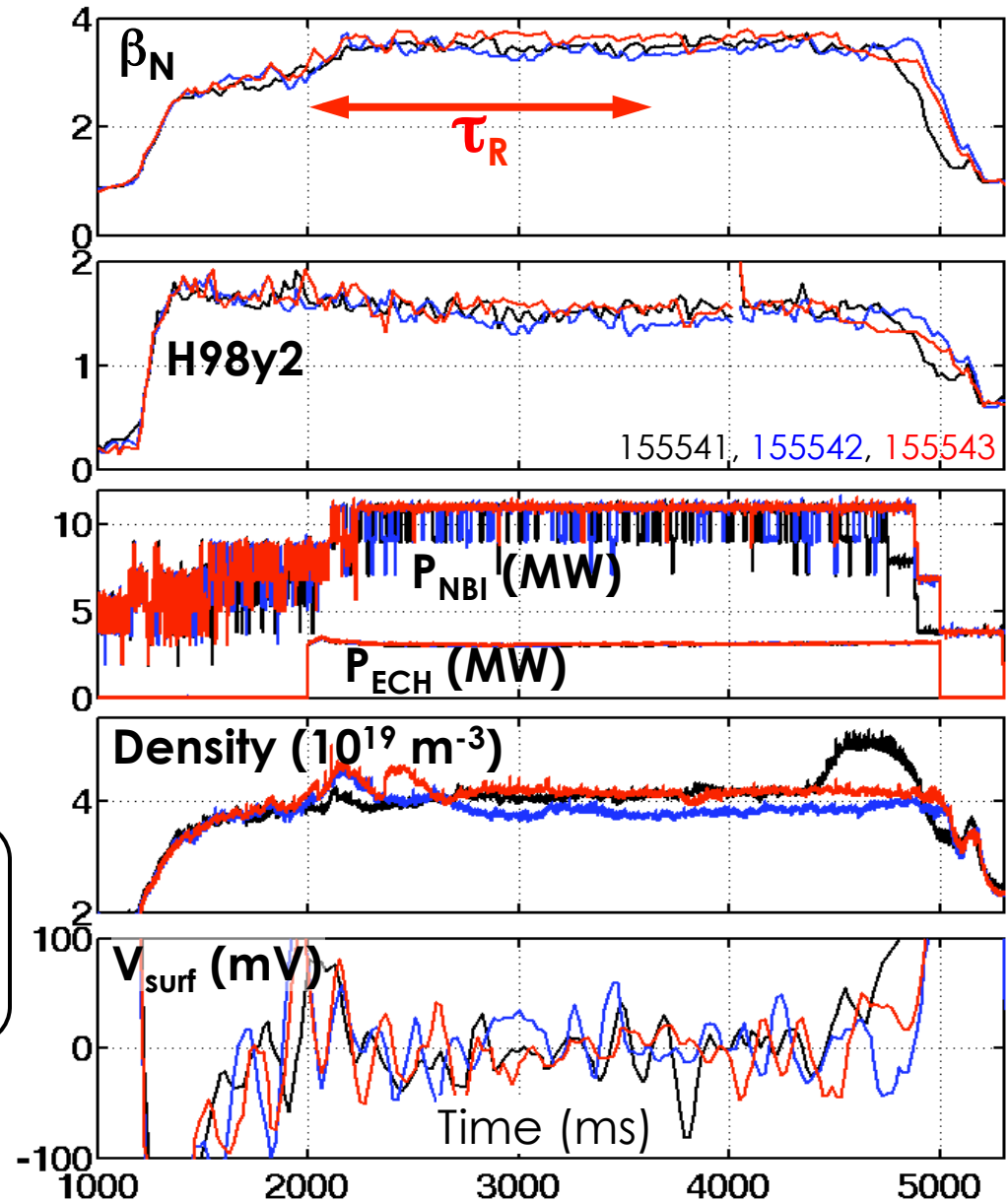
Hybrid Plasmas Reach Fully NI Conditions and $\beta_n=3.6$ for $\sim 2 \tau_r$

EXP

Double null plasma shape



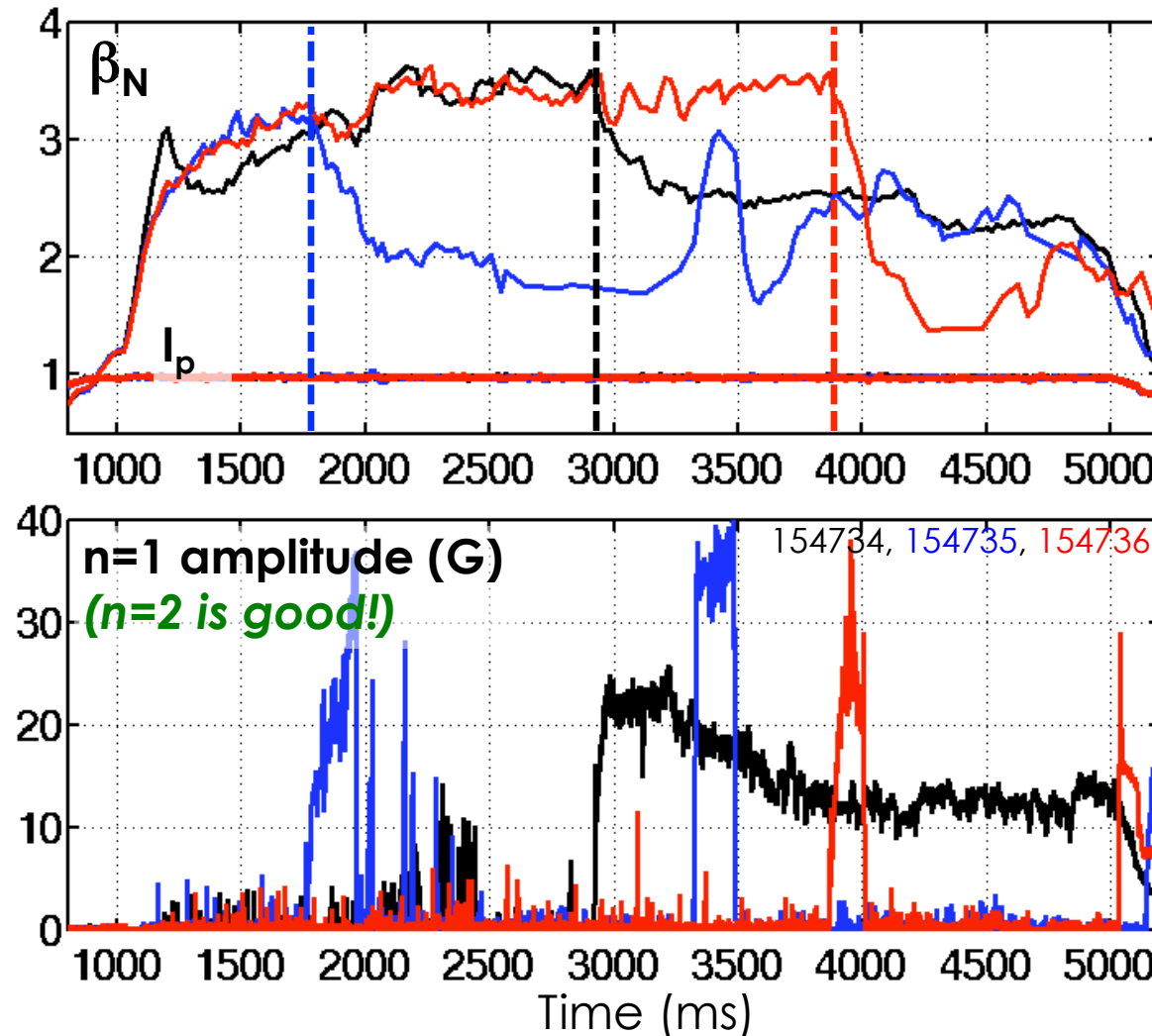
- Stable to the 2/1 TM at $\beta_N \sim 3.6$
- Loop voltage ~ 0 for $\sim 2 \tau_R$
- Limited by NBI pulse duration



MHD Stability is the Main Challenge for High- β_n Hybrids

EXP

- **2/1 tearing modes** arise on $\beta_N > 3.5$ flattop
- They degrade the confinement significantly \rightarrow loss of 20-50% β_N

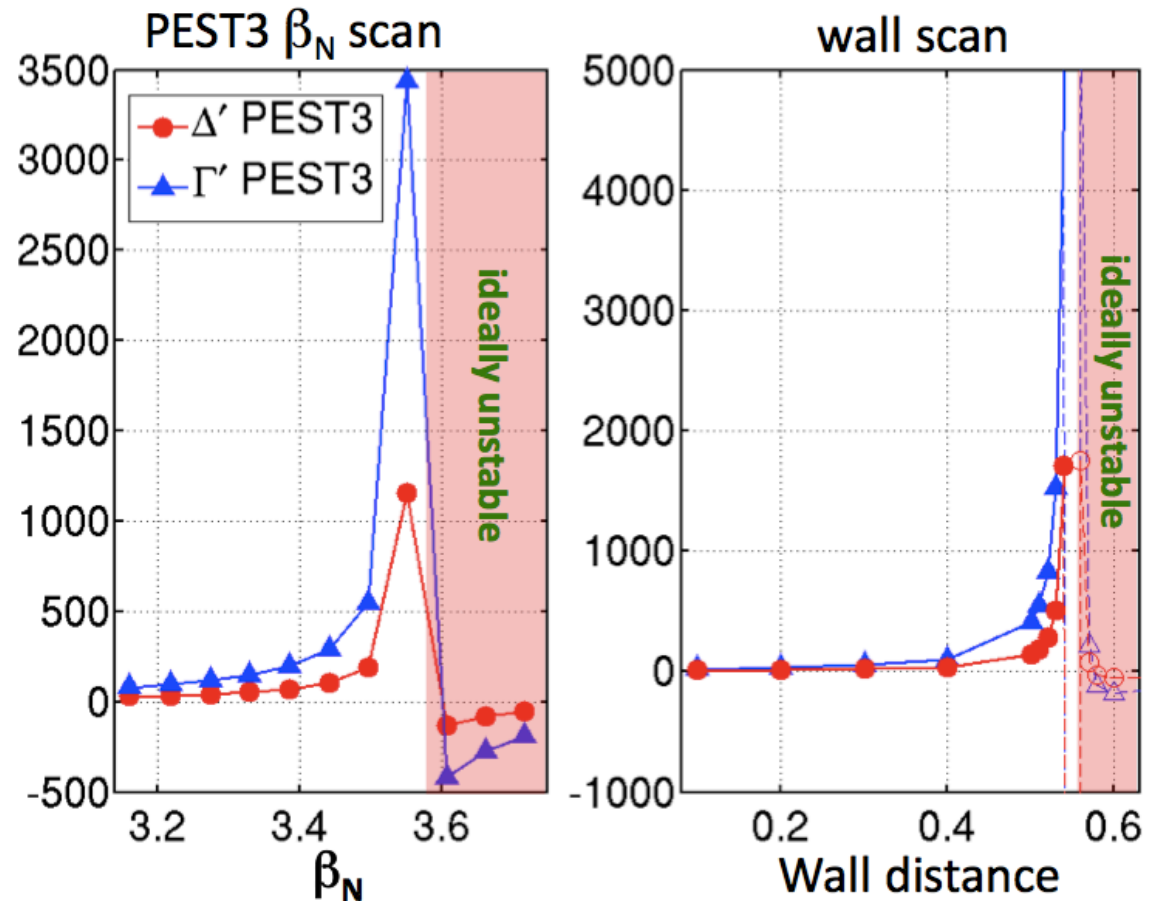


Tearing Limits Are Strongly Correlated With the Ideal With-wall Limit

MOD

- The tearing index Δ' increases sharply at the ideal wall limit

Modelling of the approach to the ideal limit:



Tearing Limits Are Strongly Correlated With the Ideal With-wall Limit

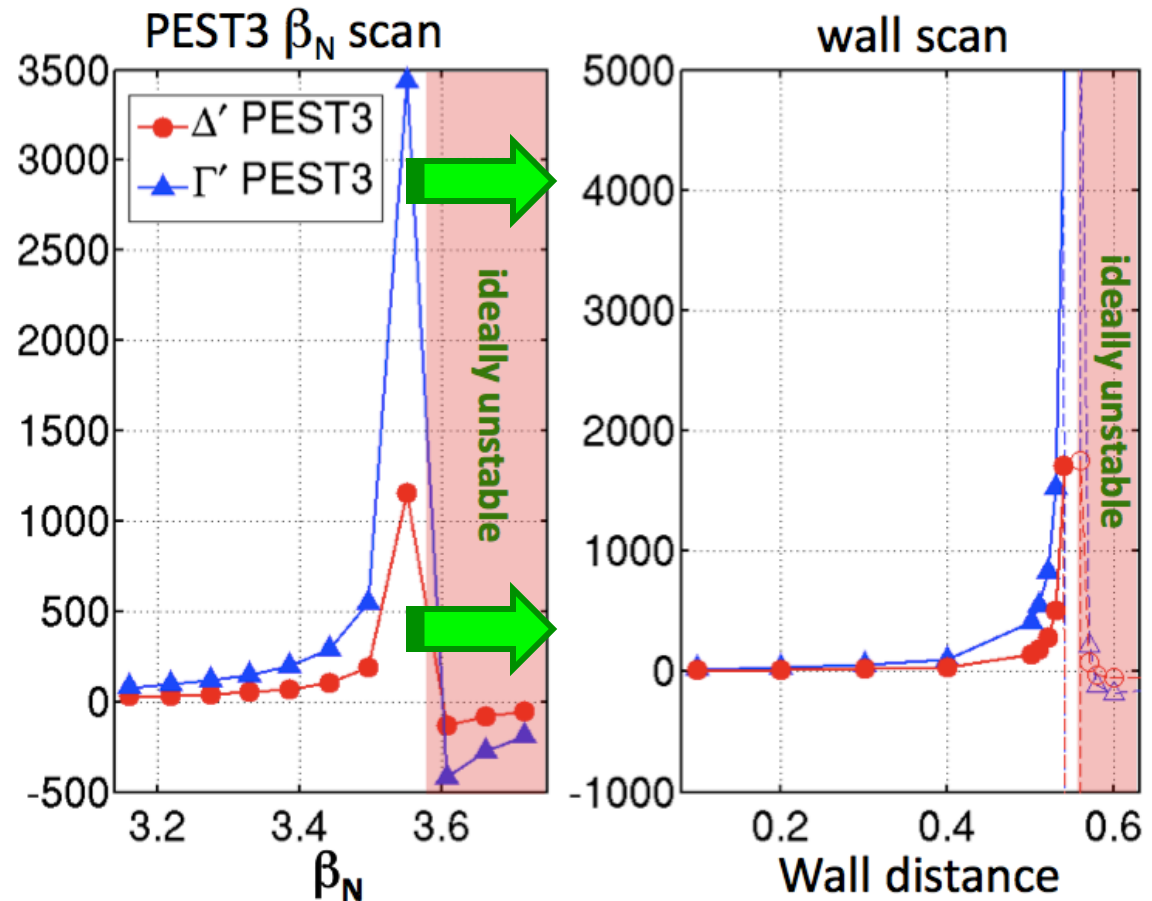
MOD

- The tearing index Δ' increases sharply at the ideal wall limit
- High β_N operation \iff Operate with very large, very sensitive Δ' ?

Modelling of the approach to the ideal limit:

One solution is to increase the ideal limit:

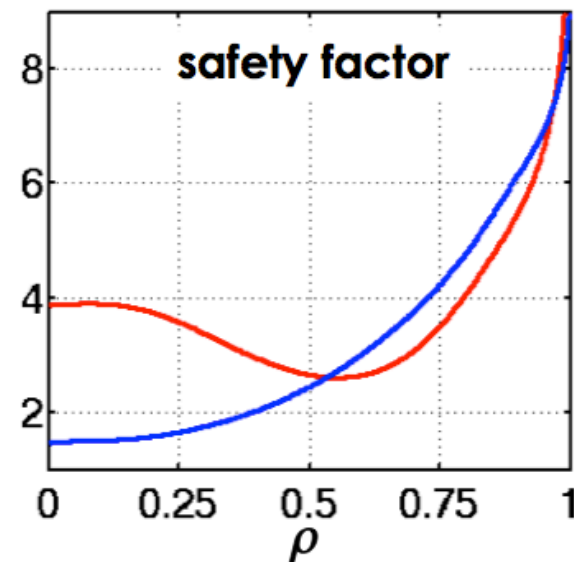
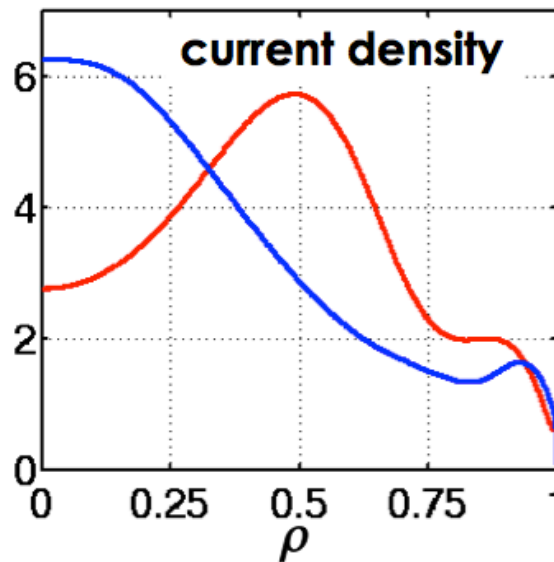
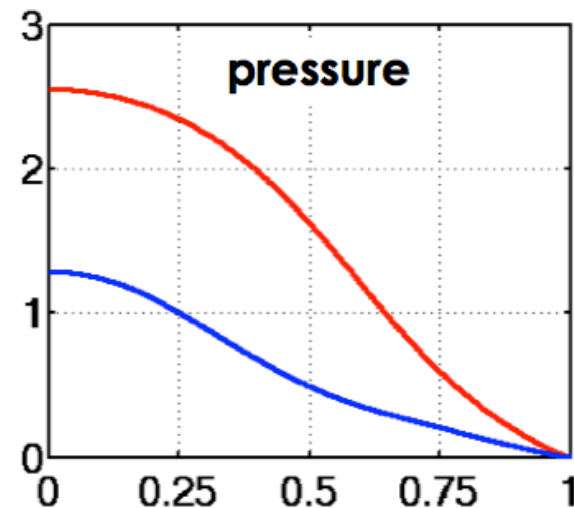
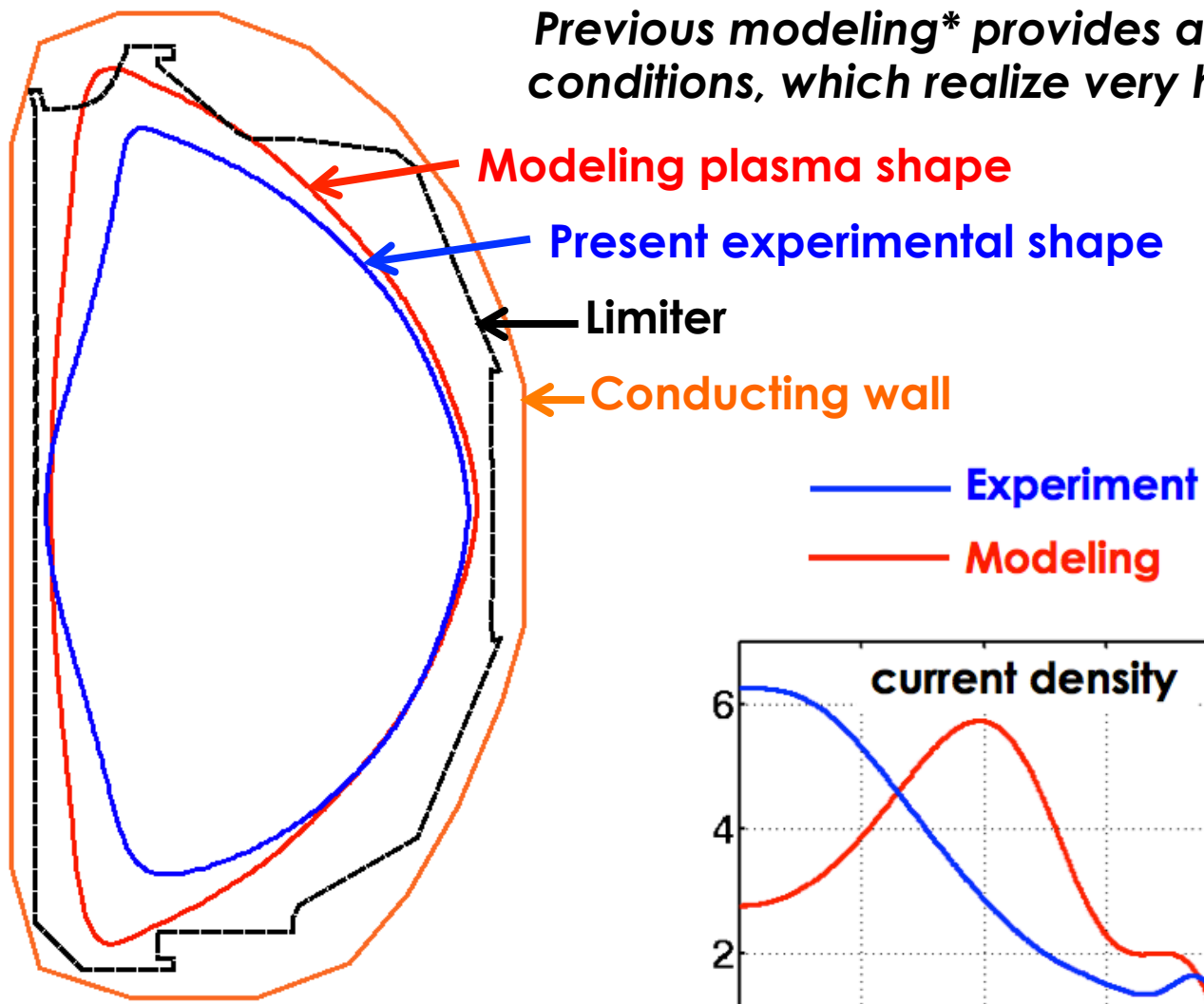
- broaden J and p
- change the plasma shape



Push the Ideal Limit Up to Improve Tearing Stability Conditions

MOD

Previous modeling provides an example of extreme conditions, which realize very high ideal stability limits*



How Much of the Increase is Due to the J and p Profiles?

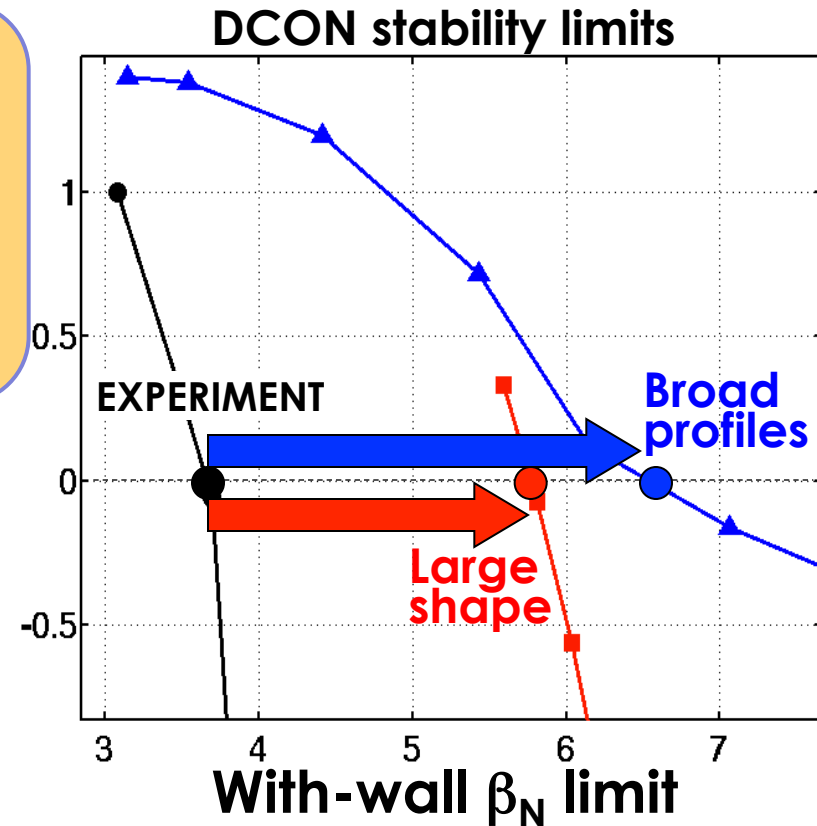
MOD

New modelling to decouple the effects:

- Experimental profiles + larger shape
- Experimental shape + broad profiles



Each makes β_{lim} \nearrow +60%



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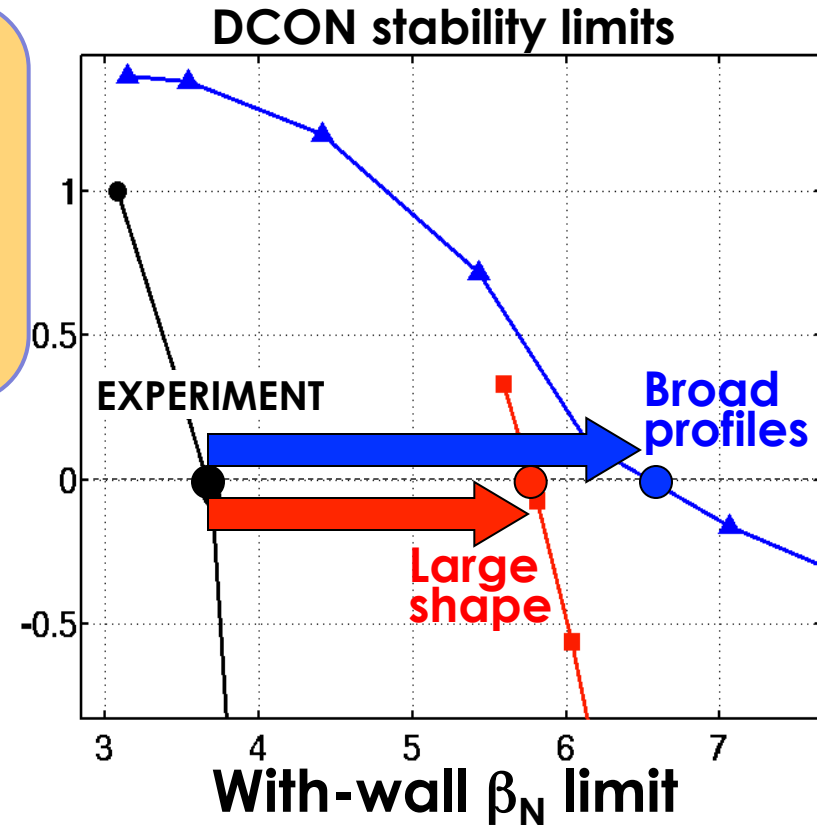
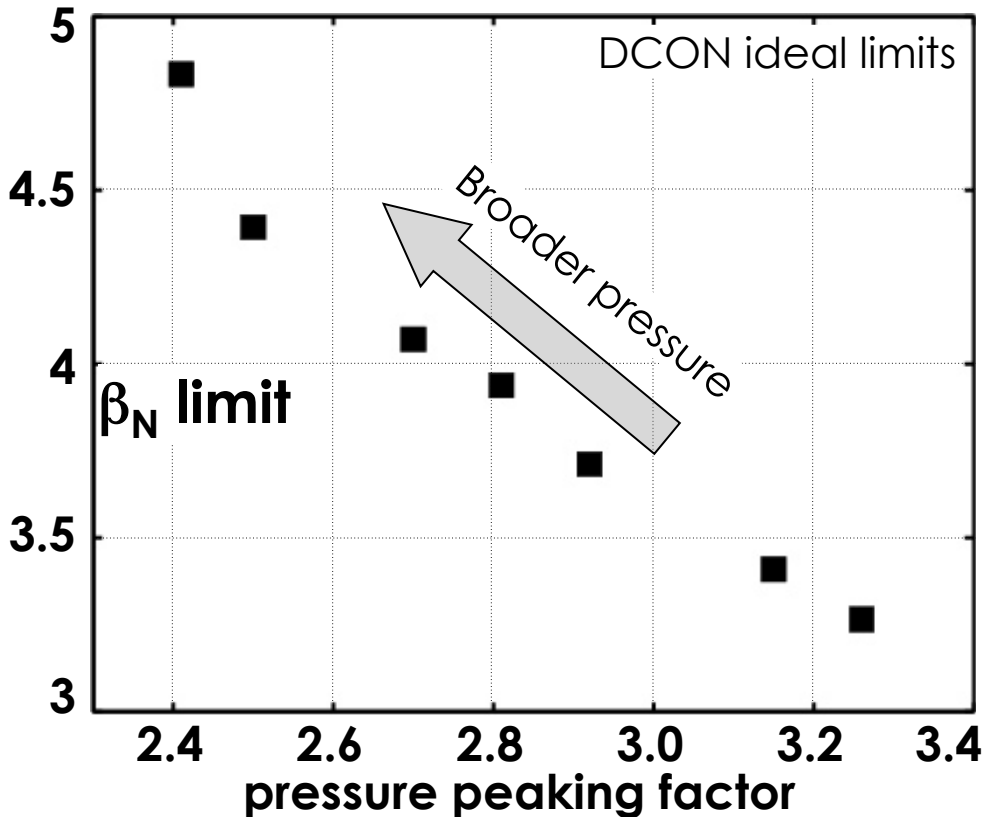
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Pressure peaking factor alone:

- Ideal $\beta_{lim} \nearrow +45\%$

How Much of the Increase is Due to the J and p Profiles?

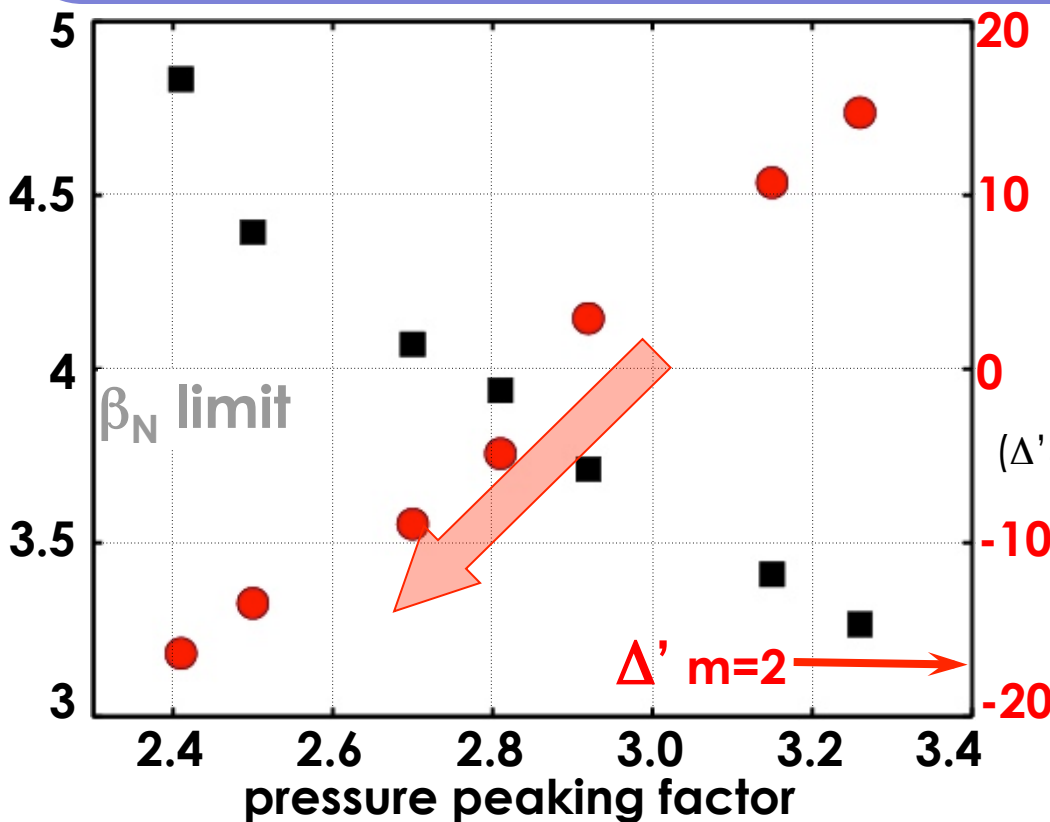
MOD

New modelling to decouple the effects:

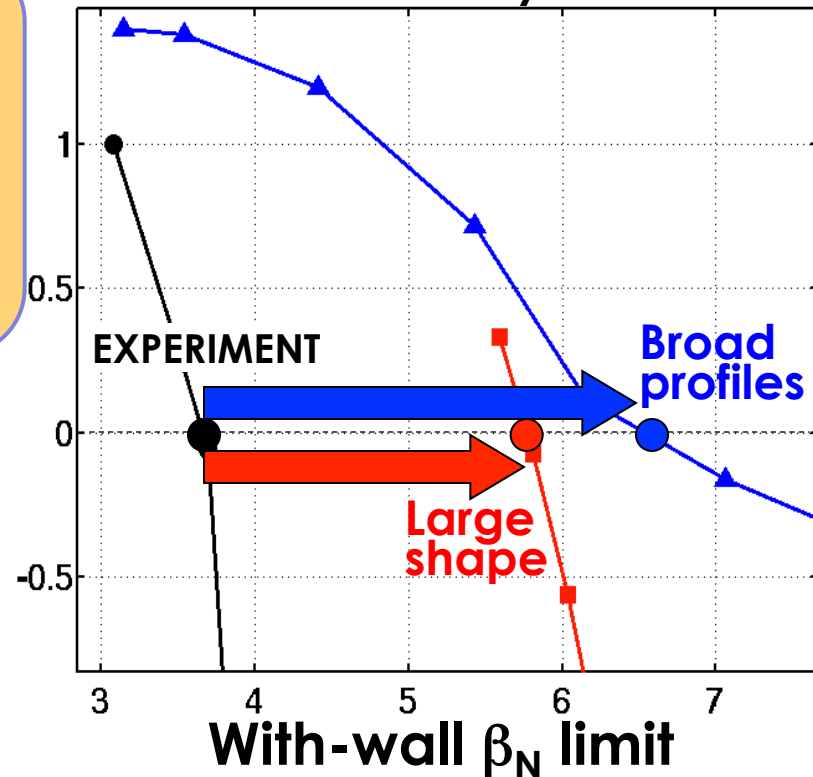
- Experimental profiles + larger shape
- Experimental shape + broad profiles



Each makes $\beta_{lim} \nearrow +60\%$



DCON stability limits



($\Delta' > 0$ necessary but not sufficient for instability)

Pressure peaking factor alone:

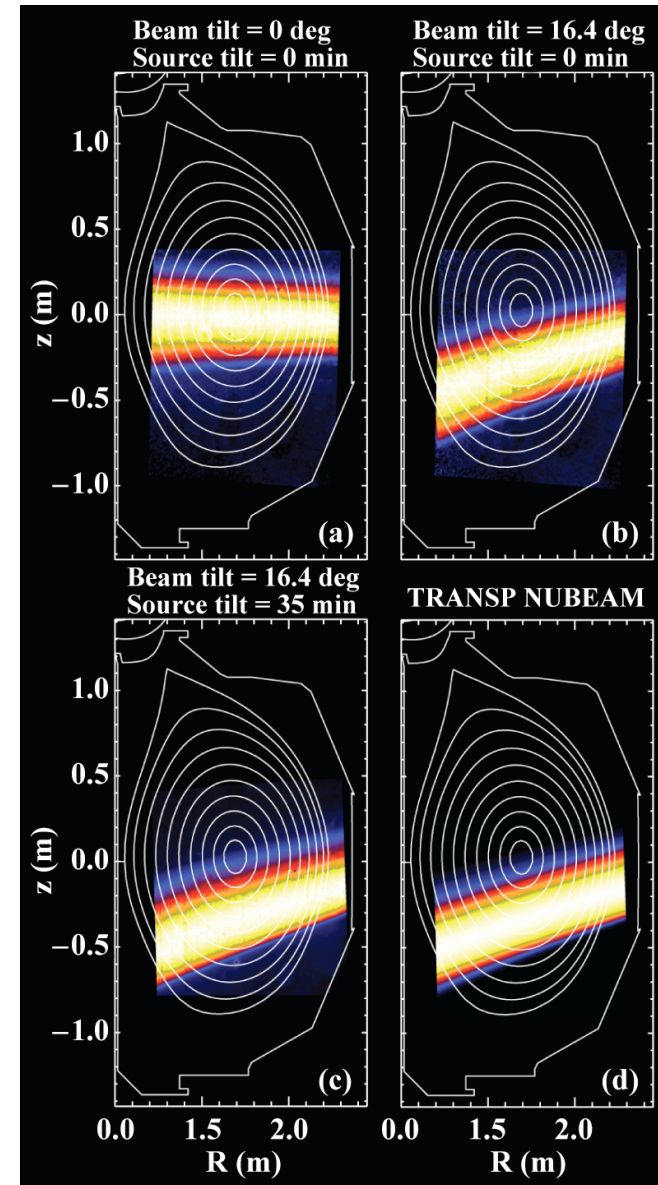
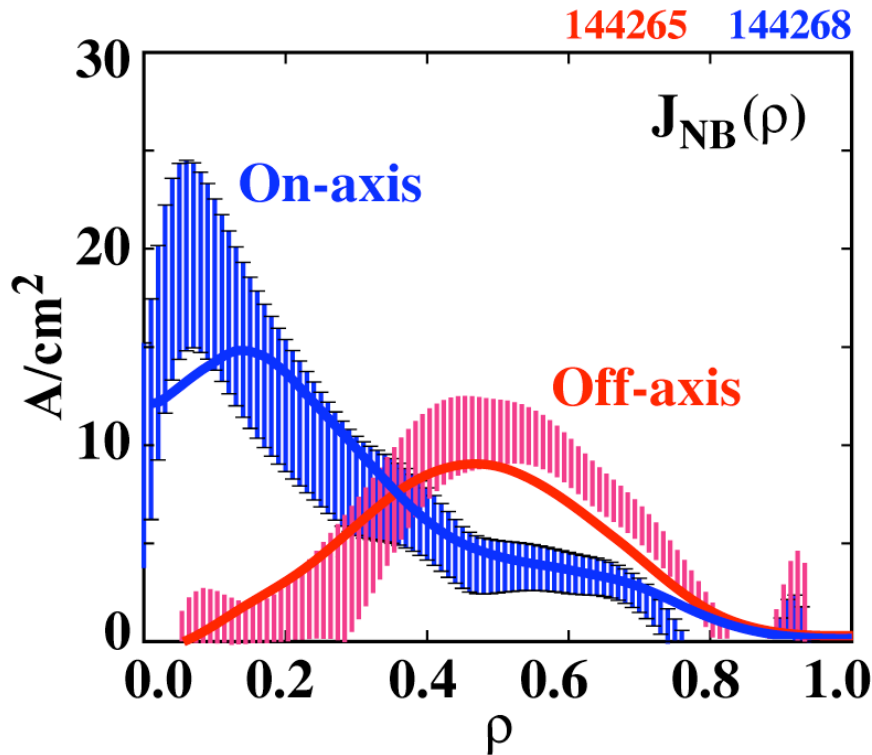
- Ideal $\beta_{lim} \nearrow +45\%$
- Tearing stability **increases m=2**

Use the Modelling Results to Design More Stable Plasmas

EXP

OFF-axis NBI to broaden the hybrid current and pressure profiles

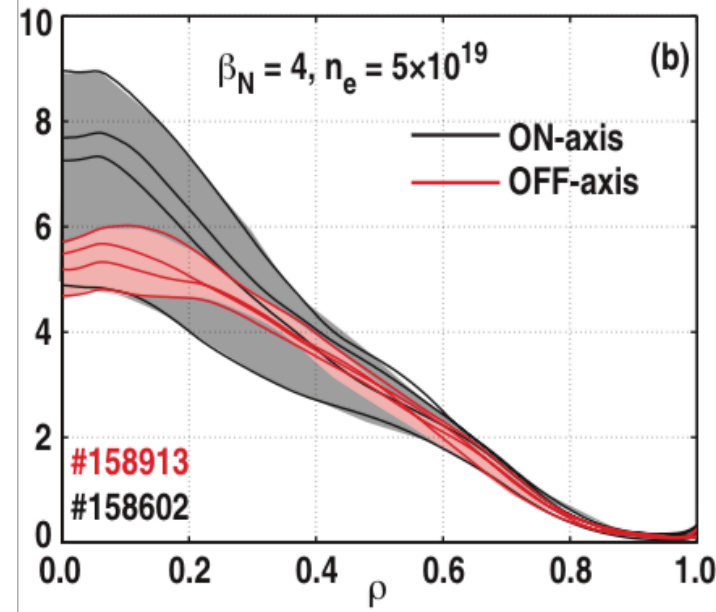
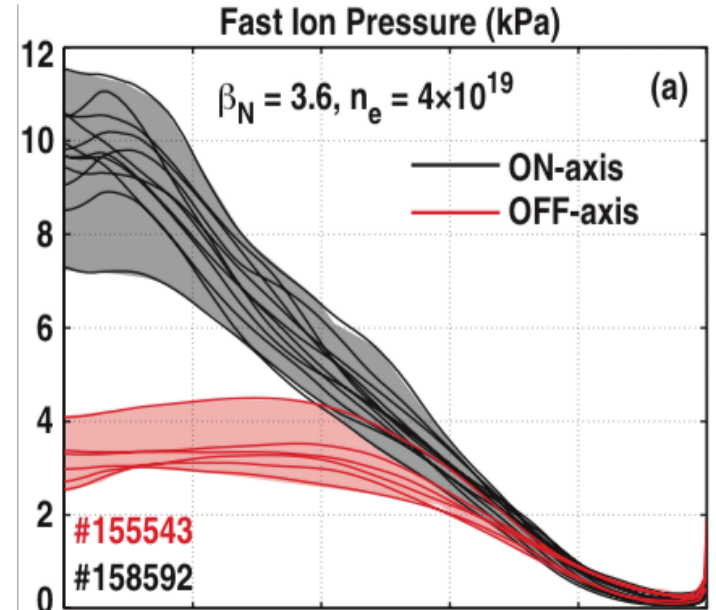
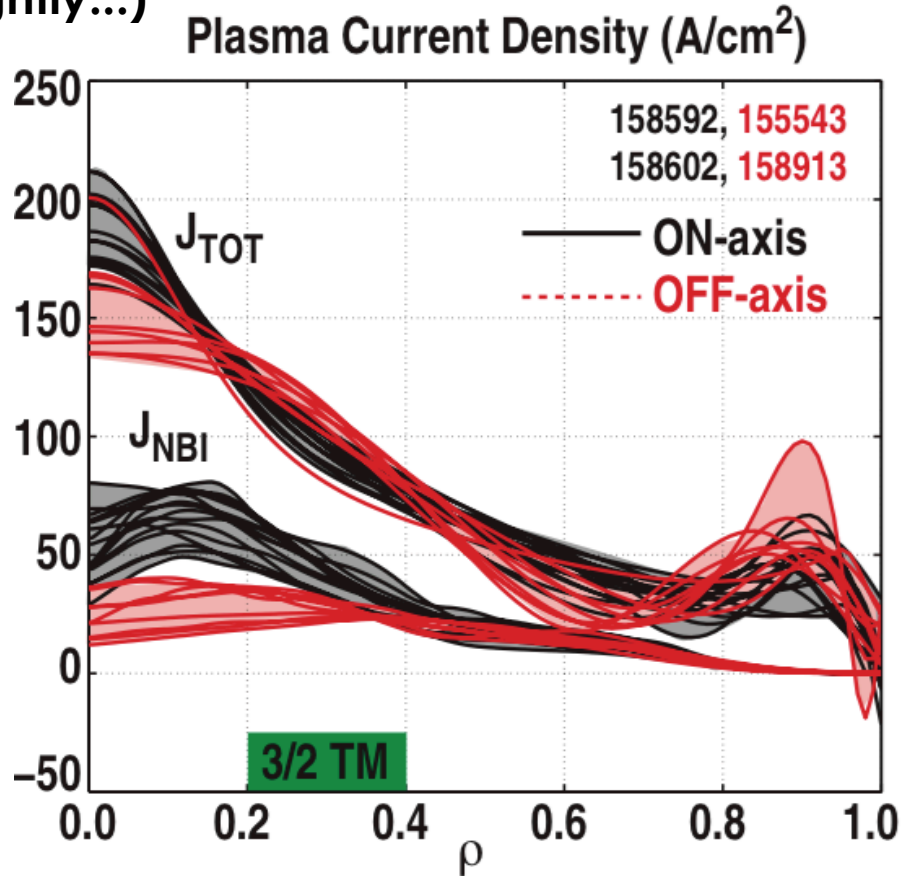
(1 neutral beam line is tilted \rightarrow ~4 MW off-axis power)



Apply this Concept to the $q_{\min} \sim 1$ Hybrid Plasmas

EXP

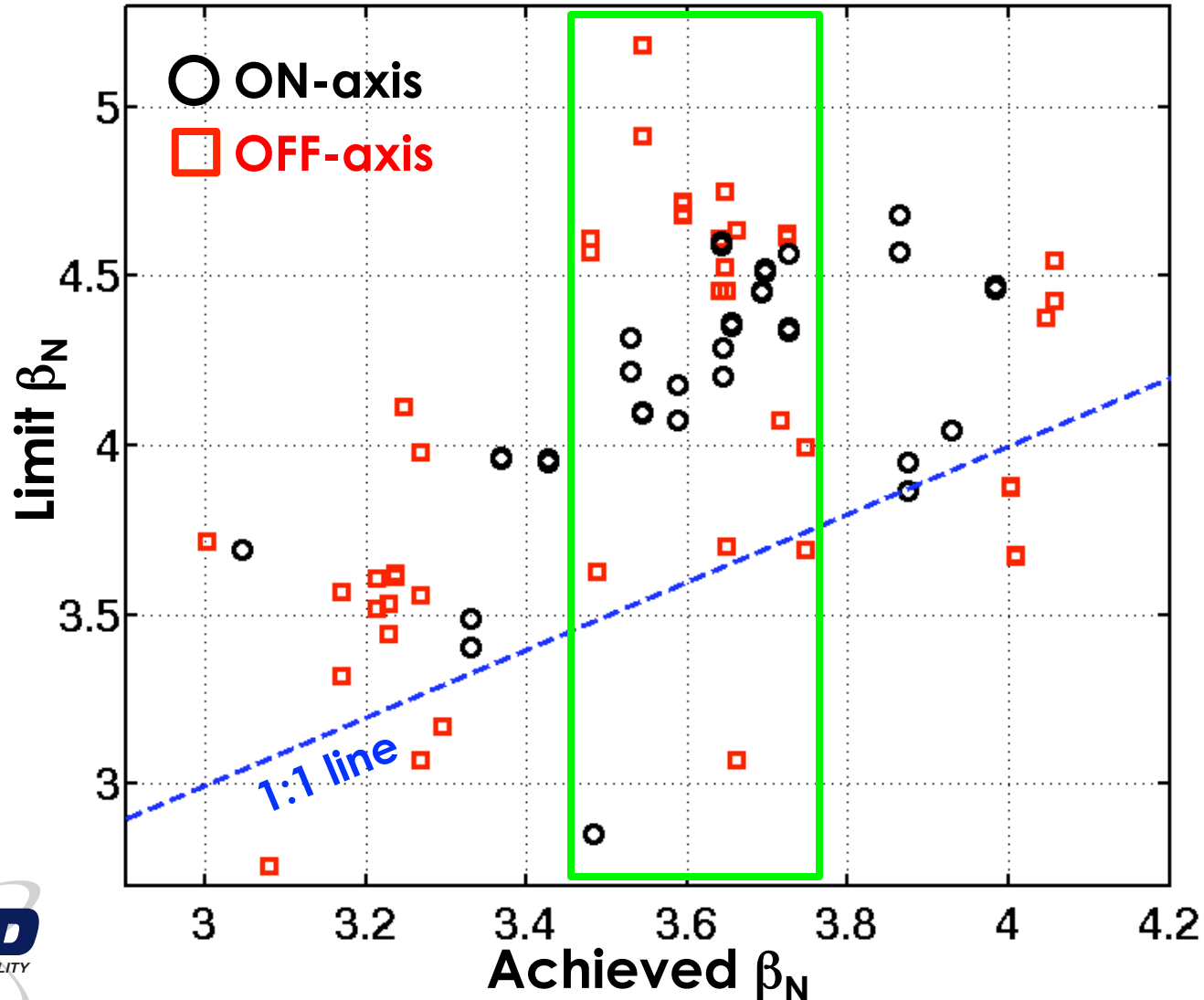
Despite the anomalous current diffusion in hybrids, 4 MM of off-axis NBI broaden J and p (slightly...)



Plasmas with **Off-axis NBI** Have Similar Ideal Limits as the On-axis Cases

EXP

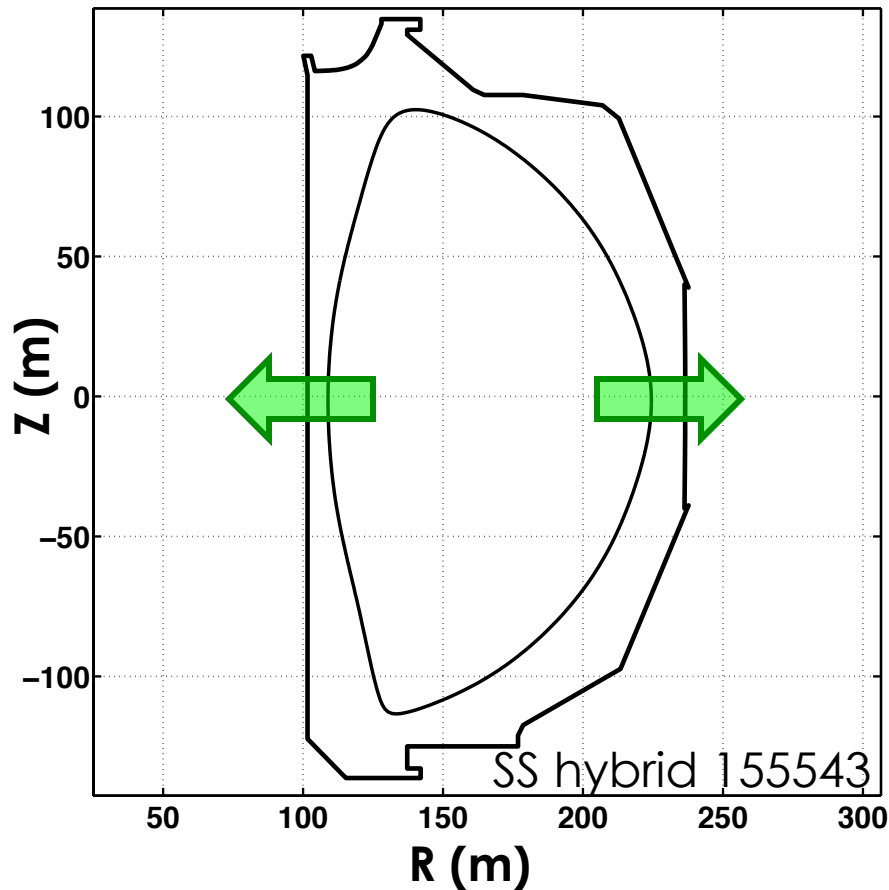
- The with-wall β_N limits of the OFF-axis cases are **~10% higher**



The Plasma Shape Can Be Optimized to Yield Higher Ideal Limits

MOD

The modelling will guide the design of the next hybrid experiment



Increase the minor radius



Decrease the inner and outer gaps



Increase the degree of wall stabilization
(within the new wall geometry limits)

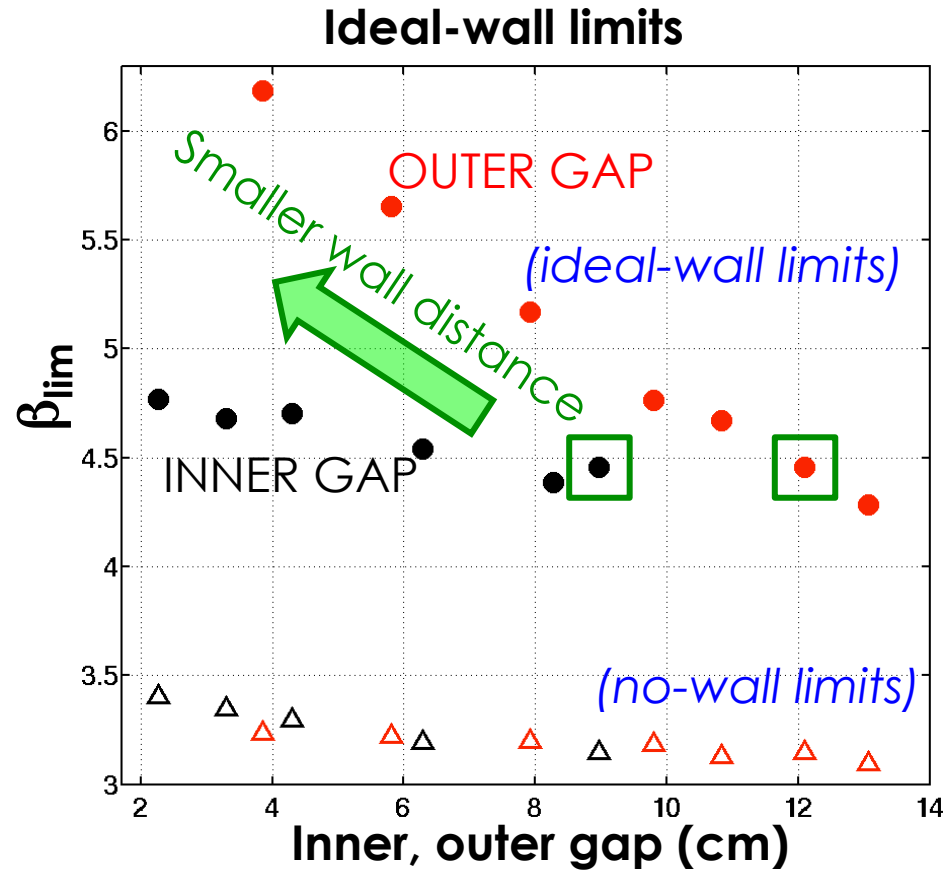
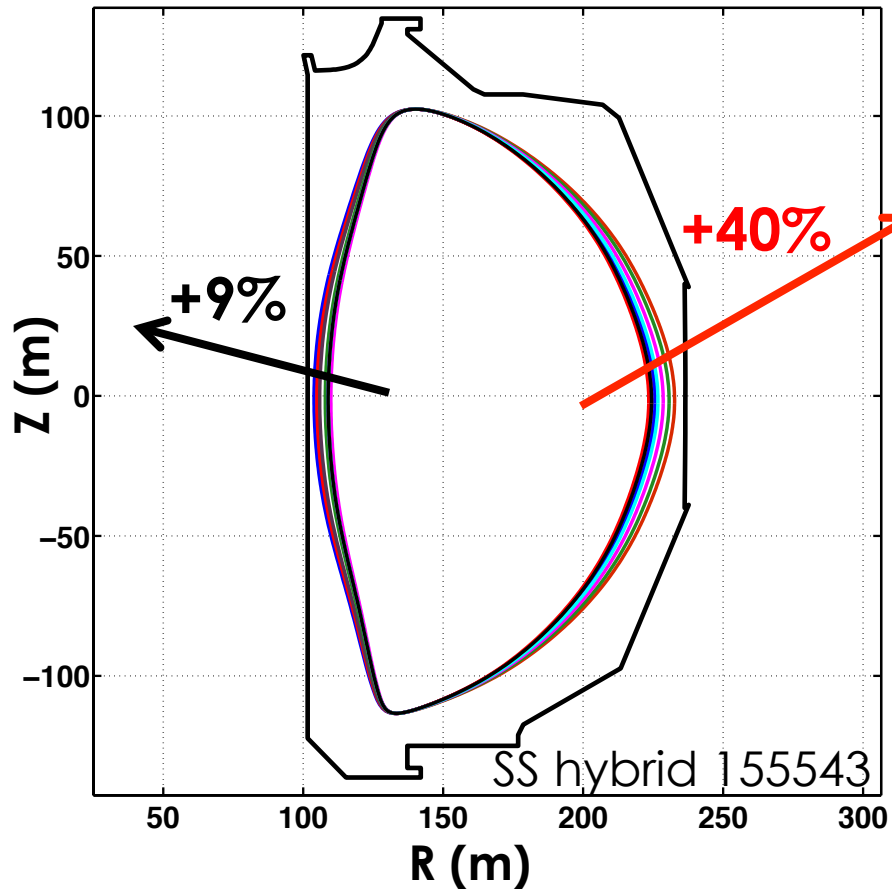
Kink structure is localised on the LFS
Does the inner gap matter?

F. Carpanese, Politecnico di Milano

Wider Shape, with Larger Squareness, will be Proposed for the Next Hybrid Experiments

MOD

The LFS wall stabilization (**outer gap**) is stronger than the HFS (inner gap)



F. Carpanese, Politecnico di Milano

All the High- β_n Plasmas Have High NBI Torque

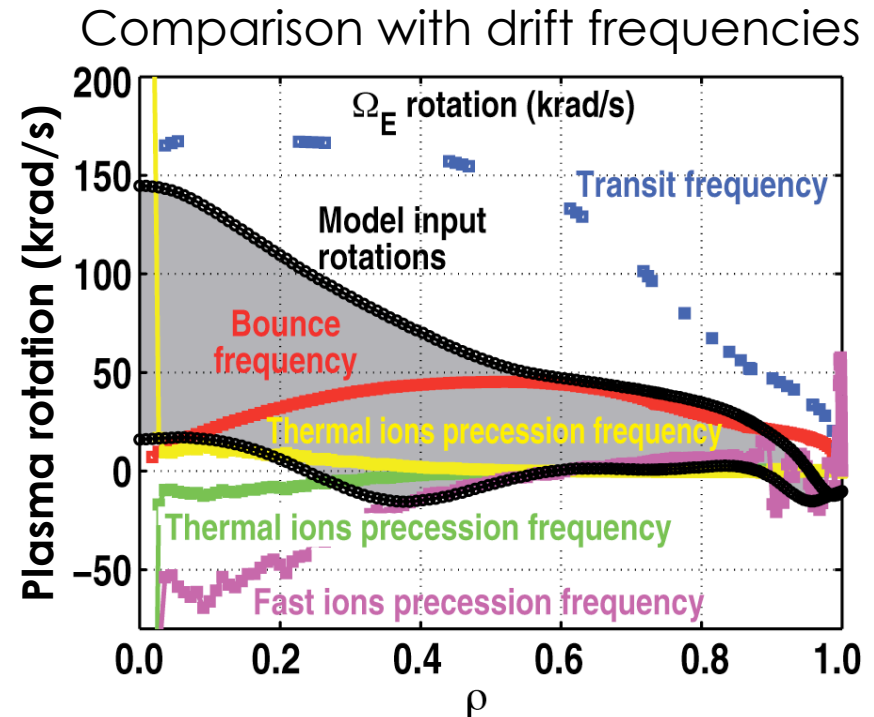
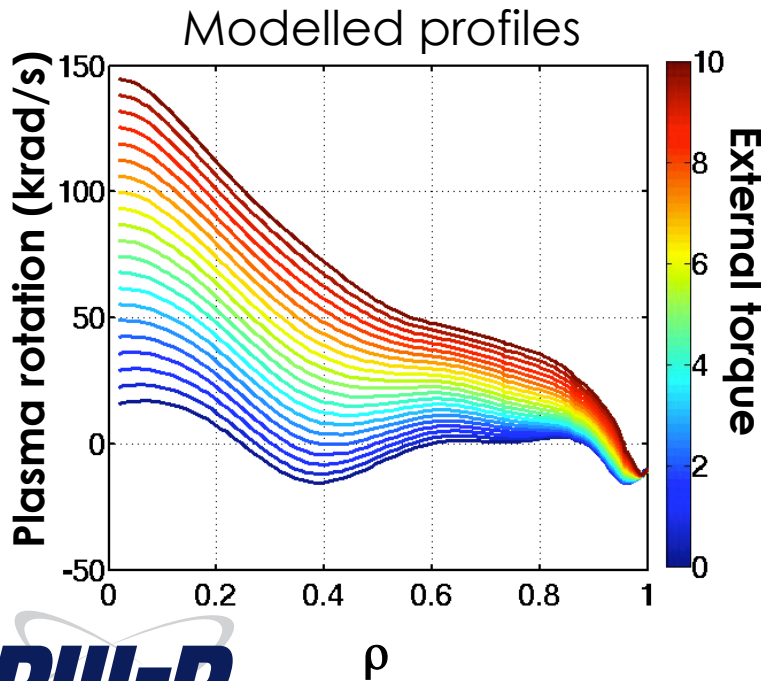
MOD

What happens at low rotation, high β_n ?

- **Experiment** \rightarrow decrease the rotation at fixed β_n , q_{95}
- **Model** \rightarrow capture the rotation effects to extrapolate what we can't do

To eliminate perturbations due to equilibrium and profile details, the model uses:

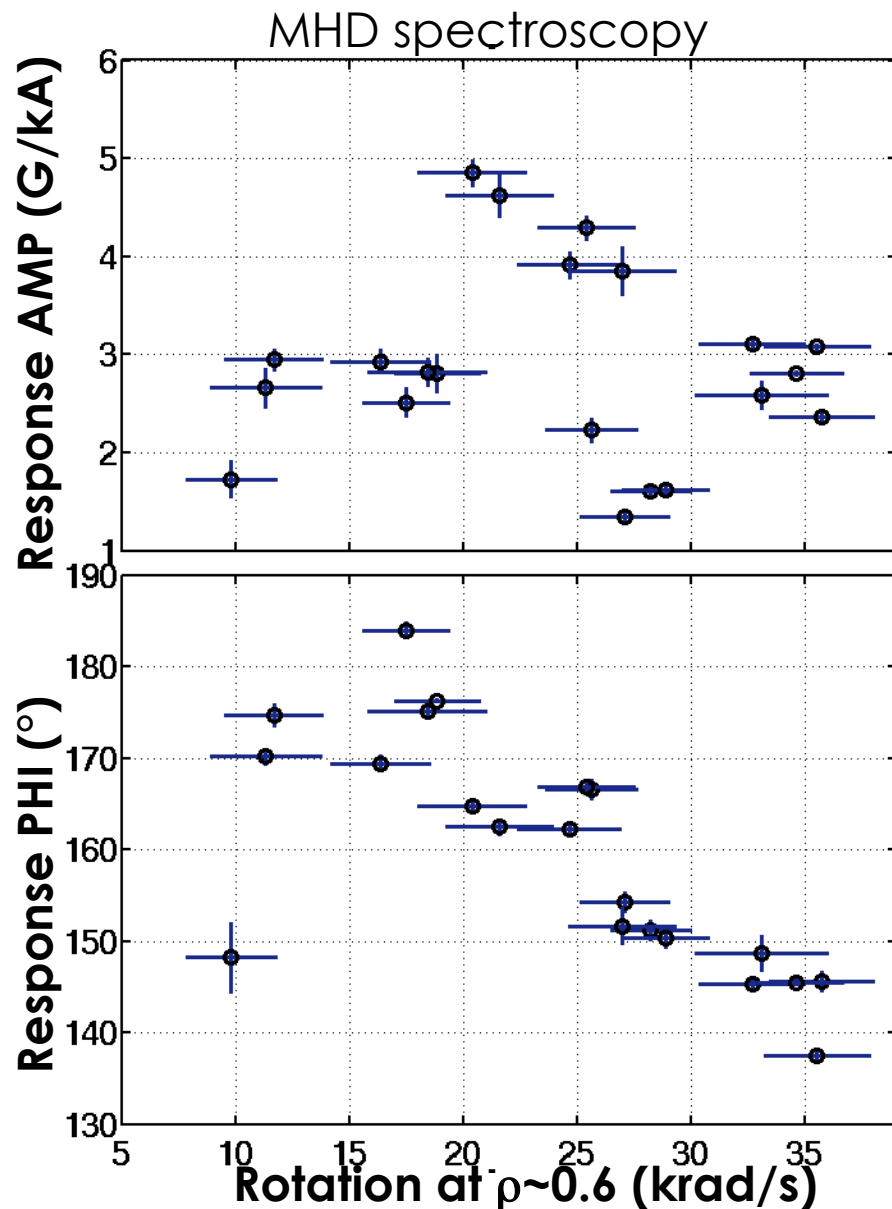
- A fixed equilibrium and n_e , T_e , n_i , P_{NBI} , etc, from a DIII-D plasma
- A self-similar rotation profile series



Rotation Effects Above the No-wall β_n Limit

EXP

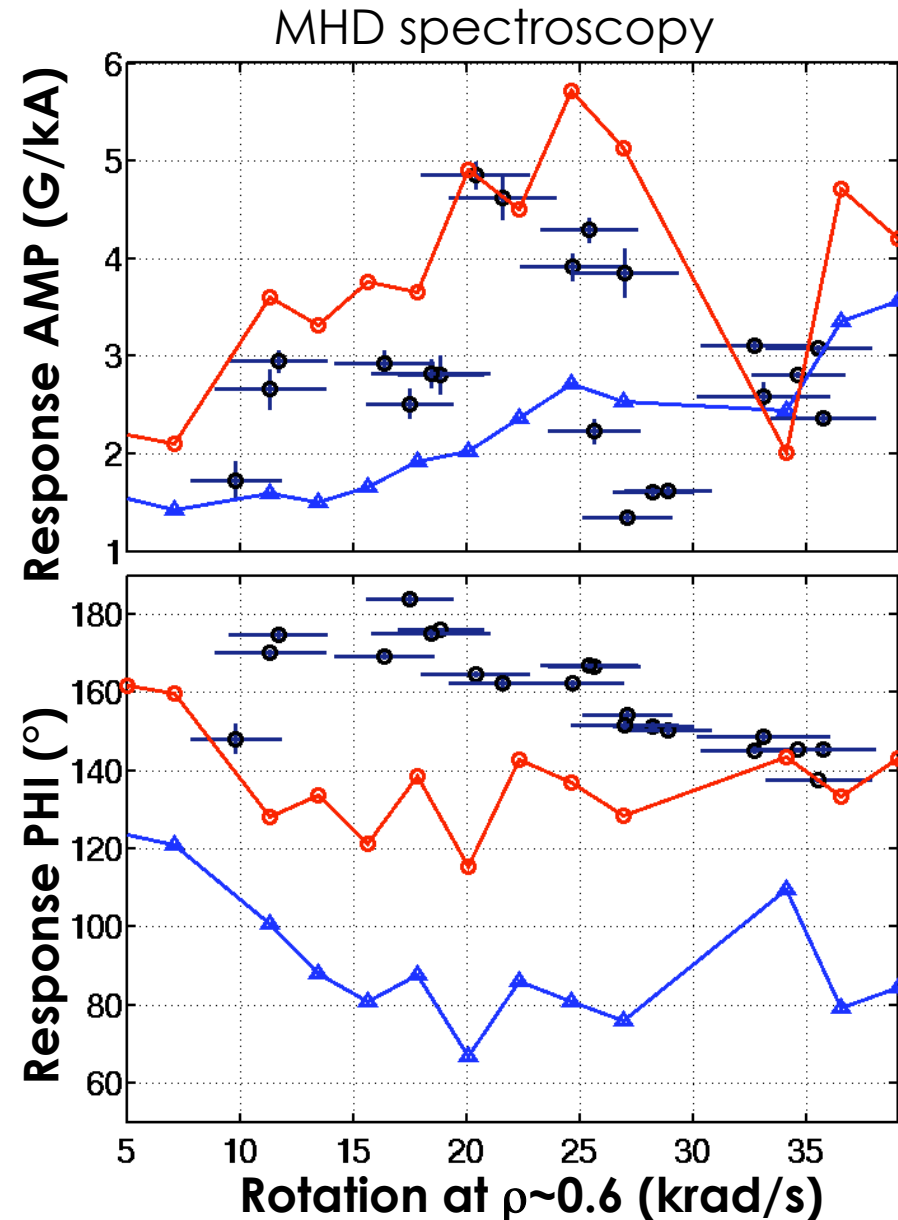
- Broad peak in the response at 20-25 km/s ($\sim 1\%$ of the Alfvén velocity)
- Below the no-wall limit (IBS) the trend is increasing



Rotation Scan: MARS-K Reproduces the Response Amplitude with Fast-ions

MOD

- With **thermal and fast ions** the amplitude results are in the ball-park
- ...but the phase is underestimated by ~25%
- If the **fast-ions damping is neglected**, the results diverge (more) from the measurements

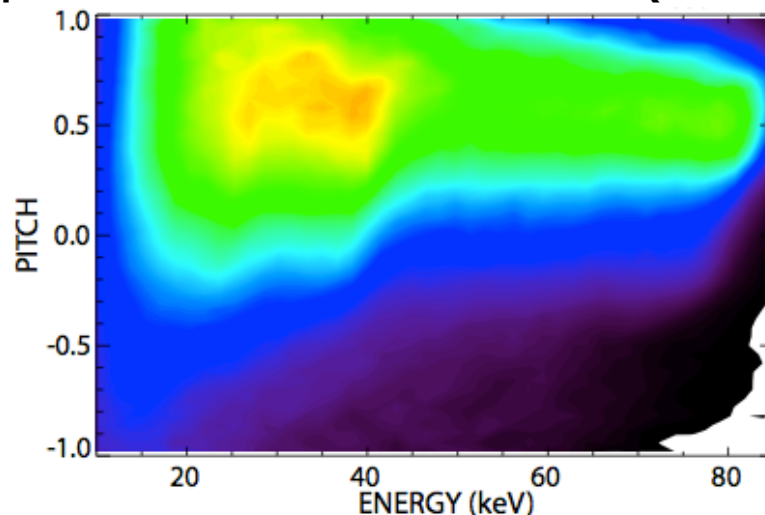


No Model is Perfect — the Way Forward

Identify what physics is not present and could be relevant:

- **Zero collisionality** → **New MARS-Q**: energy dependent collisionality operator
- **The present version of MARS-K assumes a Maxwellian fast-ion distribution** (experimental profile in ρ , but no $v_{//}$, v_{perp} dependence)
- **Neutral beam ions in DIII-D are strongly anisotropic:**

Experimental beam-ion distribution (NUBEAM)



New MARS-Q version with more realistic distribution
→ resolve the rotation scan discrepancy?

Discussion and Conclusions

- The development of viable scenarios for ITER and FNSF is based on experiments and modelling efforts
- The **ITER Baseline Scenario**: the zero torque regime operates on a marginal stability point
- **MHD spectroscopy can measure the approach to a stability limit**
 - Warning tool for disruption avoidance?
- The **MARS-K model reproduces the plasma response measurements up to the no-wall limit**
 - Fast NBI-ion damping is crucial above 90% of the limit
- The **steady-state hybrid scenario**: attractive solution for ITER and FNSF, the **ideal and tearing limits can be increased**
- **The rotation dependence at high β_N is challenging**
 - New version of MARS-K includes more physics